Machine Learning

Greedy Local Search

With slides from Bryan Pardo, Stuart Russell

ML in a Nutshell

- Every machine learning algorithm has three components:
 - Representation
 - E.g., Decision trees, instances
 - Evaluation
 - E.g., accuracy on test set

– Optimization

• How do you **find** the best hypothesis?

Hill-climbing (greedy local search)



Greedy local search needs

- A "successor" function Says what states I can reach from the current one. Often implicitly a distance measure.
- An objective (error) function Tells me how good a state is
- Enough memory to hold
 The best state found so far
 The current state
 The state it's considering moving to

Hill-climbing search

"Like climbing Everest in thick fog with amnesia"

```
function HILL-CLIMBING(problem) returns a state that is a local maximum
inputs: problem, a problem
local variables: current, a node
neighbor, a node
current \leftarrow MAKE-NODE(INITIAL-STATE[problem])
loop do
neighbor \leftarrow a highest-valued successor of current
if VALUE[neighbor] \leq VALUE[current] then return STATE[current]
current \leftarrow neighbor
```

Hill-climbing (greedy local search)

"Like climbing Everest in thick fog with amnesia"



Hill-climbing (greedy local search)

It is easy to get stuck in local maxima



Example: n-queens

 Put *n* queens on an *n* × *n* board with no two queens on the same row, column, or diagonal

Greedy local search needs

- A "successor" (distance?) function Any board position that is reachable by moving one queen in her column.
- An optimality (error?) measure How many queen pairs can attack each other?

Hill-climbing search: 8-queens problem



• *h* = number of pairs of queens that are attacking each other, either directly or indirectly

Hill-climbing search: 8-queens problem



• A local minimum with h = 1

Simulated annealing search

 Idea: escape local maxima by allowing some "bad" moves but gradually decrease their frequency

Properties of simulated annealing

- One can prove: If *T* decreases slowly enough, then simulated annealing search will find a global optimum with probability approaching 1
- Widely used in VLSI layout, airline scheduling, etc

Local beam search

- Keep track of *k* states rather than just one
- Start with *k* randomly generated states
- At each iteration, all the successors of all *k* states are generated
- If any one is a goal state, stop; else select the *k* best successors from the complete list and repeat.

Let's look at a demo



Results on 8-queens

	Random	Sim Anneal	Greedy
	600+	173	4
	15	119	4
	154	114	5
Average	256+	135	4

• Note: on other problems, your mileage may vary

Continuous Optimization

- Many AI problems require optimizing a function f(x), which takes continuous values for input vector x
- Huge research area
- Examples:
 - Machine Learning
 - Signal/Image Processing
 - Computational biology
 - Finance
 - Weather forecasting
 - Etc., etc.

Gradient Ascent

- Idea: move in direction of steepest ascent (gradient)
- $\mathbf{x}_k = \mathbf{x}_{k-1} + \eta \nabla f(\mathbf{x}_{k-1})$



Types of Optimization

- Linear vs. non-linear
- Analytic vs. Empirical Gradient
- Convex vs. non-convex
- Constrained vs. unconstrained

Continuous Optimization in Practice

- Lots of previous work on this
- Use packages

Final example: weights in NN



 $d(x, y) = (x_1 - y_1)^2 + (x_2 - y_2)^2 \quad d(x, y) = (x_1 - y_1)^2 + (3x_2 - 3y_2)^2$

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