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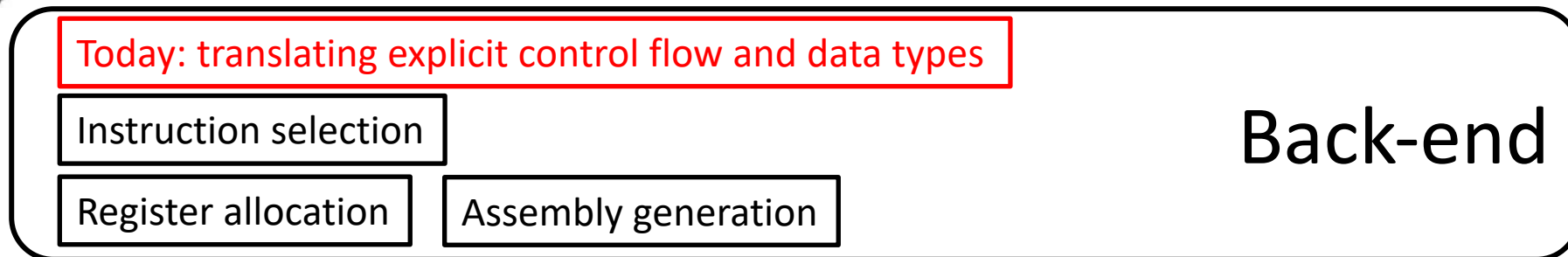
Outline

- IR
- Linearize the CFG
- Linearize the data types

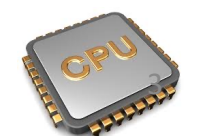
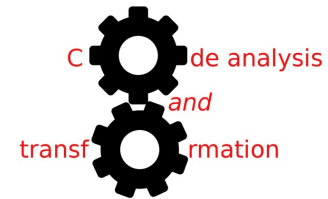
A compiler



High level programming language



Machine code



For simple data types (e.g., int64)
and simple control flows (e.g., straight line code),
L3 and IR are very similar

L3

```
define @main (){  
  %myRes <- call @myF(5)  
  %v1 <- %myRes * 4  
  %v2 <- %myRes + %v1  
  return  
}  
define @myF (%p1){  
  %p2 <- %p1 + 1  
  return %p2  
}
```

IR

```
define void @main (){  
  :entry  
  int64 %myRes  
  int64 %v1  
  int64 %v2  
  %myRes <- call @myF(5)  
  %v1 <- %myRes * 4  
  %v2 <- %myRes + %v1  
  return  
}  
define int64 @myF (int64 %p1){  
  :myLabel  
  int64 %v0  
  %v0 <- %p1 + 1  
  return %v0  
}
```

For simple data types (e.g., int64)
and simple control flows (e.g., straight line code),
L3 and IR are very similar

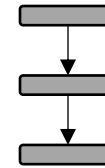
L3 and IR start to differ when we use
more complex data types (e.g., multi-dimensional arrays)
and more complex control flows (e.g., conditional branches)

IR features

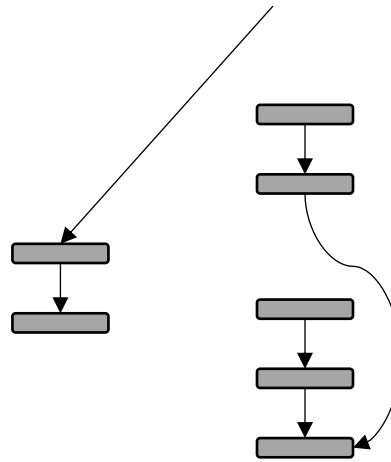
- The IR is a language designed for
 - The rich set of code analyses and transformations included in the middle-end of a compiler
 - Decoupling between source language-specific aspects and architecture-specific aspects
 - It does not imply portability
- Motivation
 - The middle-end job: **analyze, analyze, analyze**, and transform
 - To help analyzing the IR: explicit control flow
 - Liveness analysis is an example of what the middle-end does
 - Your liveness analysis had to “learn” who were the successors of an instruction
 - Successor/predecessor of an instruction: control flows
 - If I have 1000 code analyses, do they all have to “learn” the control flows?
 - Control flows need to be explicit in the code to simplify the middle-end
 - Solution: the IR language encodes computation as a graph called **Control Flow Graph (CFG)**

Representing the control flow of the program

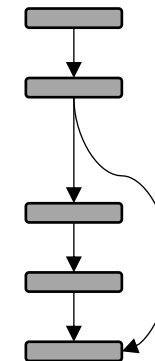
- Most instructions



- Jump instructions



- Branch instructions



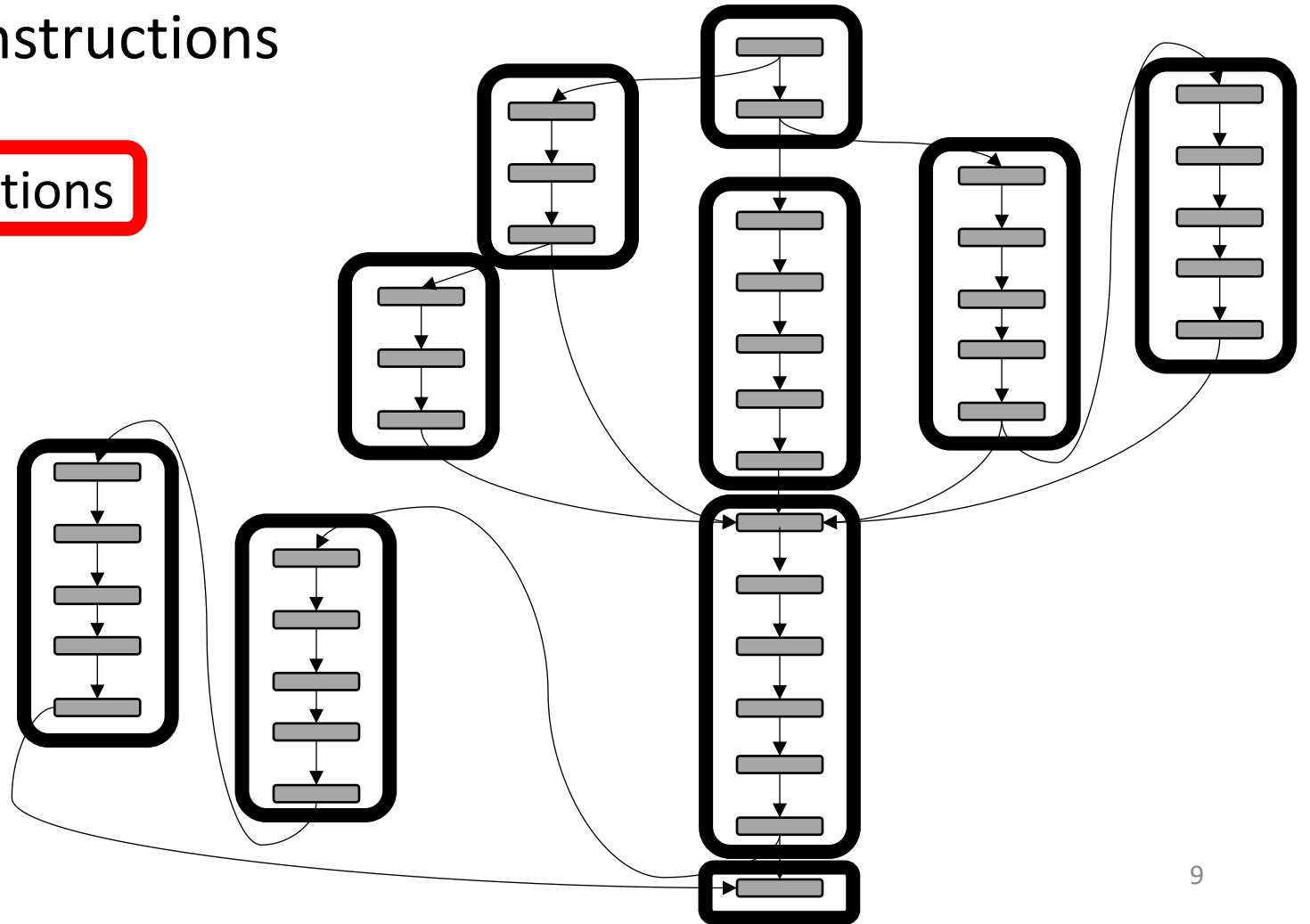
Representing the control flow of the program

A graph where nodes are instructions

- Very large
- Lot of straight-line connections
- Can we simplify it?

Basic block

Sequence of instructions that is always entered at the beginning and exited at the end

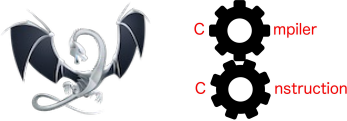


Basic blocks

A basic block is a maximal sequence of instructions such that

- Only the first one can be reached from outside this basic block
- All instructions within are executed consecutively if the first one get executed
 - Only the last instruction can be a branch/jump
 - Only the first instruction can be a label
- The storing sequence = execution order in a basic block

Basic blocks in compilers

- Automatically identified
 - Algorithm:
 - Code changes trigger the re-identification
 - Increase the compilation time
- Enforced by design 
 - Instruction exists only within the context of its basic block
 - To define a function:
 - you define its basic blocks first
 - Then you define the instructions of each basic block

L3

```
p ::= f+
f ::= define l ( vars ) { i+ }
i ::= var <- s | var <- t op t | var <- t cmp t |
    var <- load var | store var <- s |
    return | return t | label | br label | br t label |
    call callee ( args ) | var <- call callee ( args )
callee ::= u | print | allocate | input | tensor-error
vars ::= | var | var ( , var )*
args ::= | t | t ( , t )*
s ::= t | label | l
t ::= var | N
u ::= var | l
op ::= + | - | * | & | << | >>
cmp ::= < | <= | = | >= | >
N ::= (+|-)? [0-9]+
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

IR

```
p ::= f+
f ::= define T | ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
    var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
    call callee ( args? ) | var <- call callee ( args? ) |
    var <- new Array(args) | var <- new Tuple(t)
T ::= type | void
type ::= int64([])* | tuple | code
callee ::= u | print | input | tensor-error
args ::= t | t ( , t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]+
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

```
define int64 @myF (int64 %p1){
    :myLabel
    int64 %v1
    %v1 <- 1
    int64[][] %myMatrix
    int64[][][][] %myTensor
    tuple %myHeterogeneousArray
    code %myFunctionPointer
    %myFunctionPointer <- @myF
    return %v1
}
```

IR



```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
    var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
    call callee ( args? ) | var <- call callee ( args? ) |
    var <- new Array(args) | var <- new Tuple(t)
T ::= type | void
type ::= int64([])* | tuple | code
callee ::= u | print | input | tensor-error
args ::= t | t ( , t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]+
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

```
define void @main () {
    :entry
    call @myF(:i, 2)
    return
}

define int64 @myF (int64 %p1,
int64 %p2) {
    :entry
    int64 %v1
    %v1 = %p1 + %p2
    return %v1
}
```

IR



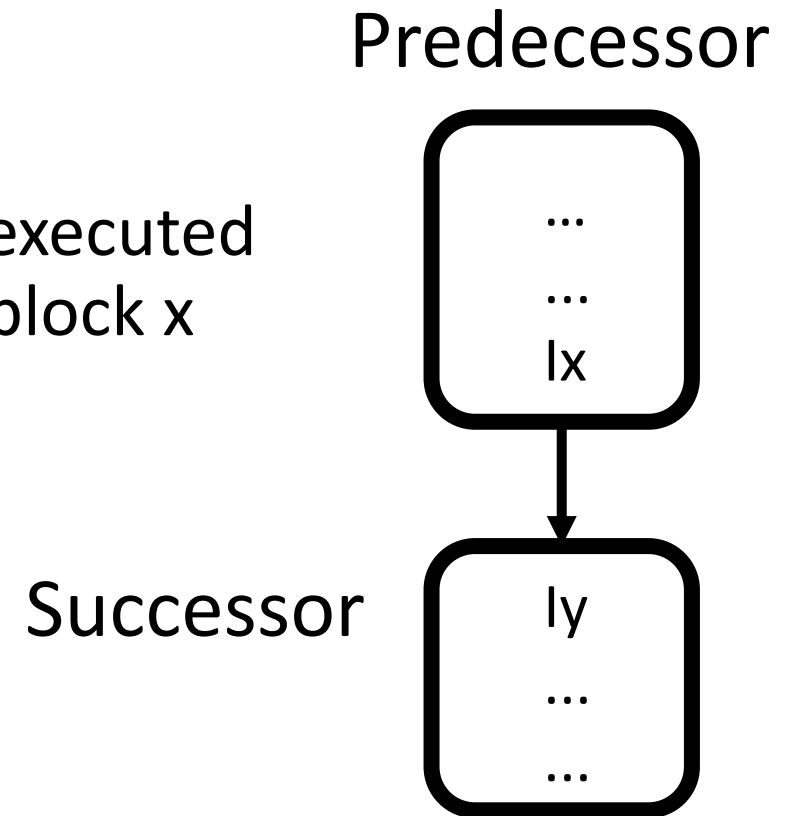
```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
    var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
    call callee ( args? ) | var <- call callee ( args? ) |
    var <- new Array(args) | var <- new Tuple(t)
T ::= type | void
type ::= int64([])* | tuple | code
callee ::= u | print | input | tensor-error
args ::= t | t ( , t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]+
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

```
define void @main () {
    call print(1)
    return
}
```

Control Flow Graph (CFG)

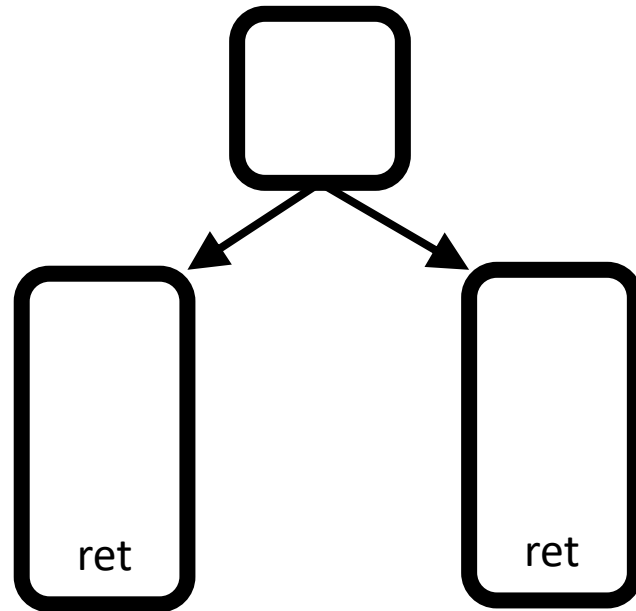
- A CFG is a graph $G = \langle \text{Nodes}, \text{Edges} \rangle$
- Nodes: Basic blocks
- Edges: $(x,y) \in \text{Edges}$ iff

first instruction in basic block y **might** be executed just after the last instruction of the basic block x



Control Flow Graph (CFG)

- Entry node: block with the first instruction of the function
- Exit nodes: blocks with the return instruction
- All basic blocks beside the first can be stored in any order




IR function is a CFG

IR encodes the CFG explicitly by

- Enforcing (in the grammar) explicit predecessor-successor relations between basic blocks
- Enforcing the first basic block is the entry point of the function

IR

```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
    var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
    call callee ( args? ) | var <- call callee ( args? ) |
    var <- new Array(args) | var <- new Tuple(t)
T ::= type | void
type ::= int64([])* | tuple | code
callee ::= u | print | input | tensor-error
args ::= t | t ( , t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]+
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```



```
define int64 @myF (int64 %p1){
    :myLabel
    int64 %c
    %c <- %p1 >= 3
    br %c :true :false

    :true
    return 1

    :false
    return 0
}
```

IR makes the CFG explicit

IR also makes complex data types explicit

- Explicit data types
- Explicit allocations

IR

p ::= f⁺
f ::= define T l ((type var)*) { bb⁺ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
 var <- var([t])⁺ | var([t])⁺ <- s | var <- length var t | var <- length var |
 call callee (args?) | var <- call callee (args?) |
 var <- new Array(args) | var <- new Tuple(t) ←

T ::= type | void
type ::= int64([])* | tuple | code *Implicit initialization to "1"*
callee ::= u | print | input | tensor-error
args ::= t | t (, t) *
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+ | -) ? [0 - 9] *
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*

```
define int64 @myF (int64 %p1){  
    :myLabel  
    int64[] %v  
    %v <- new Array(7)  
    %v[1] <- 1  
    return 0  
}
```

IR

```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
    var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
    call callee ( args? ) | var <- call callee ( args? ) |
    var <- new Array(args) | var <- new Tuple(t) ←
T ::= type | void
type ::= int64([])* | tuple | code
callee ::= u | print | input | tensor-error
args ::= t | t ( , t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]+
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

Implicit initialization to "1"

```
define int64 @myF (int64 %p1){
    :myLabel
    int64[][] %v
    %v <- new Array(7,7)
    %v[0][3] <- 1
    return 0
}
```

IR

p ::= f⁺
f ::= define T l ((type var)*) { bb⁺ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
 var <- var([t])⁺ | var([t])⁺ <- s | var <- length var t | var <- length var |
 call callee (args?) | var <- call callee (args?) |
 var <- new Array(args) | var <- new Tuple(t) ←

T ::= type | void
type ::= int64([])* | tuple | code *Implicit initialization to "1"*
callee ::= u | print | input | tensor-error
args ::= t | t (, t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]⁺
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*

```
define int64 @myF (int64 %p1){  
    :myLabel  
    int64[][][] %v  
    %v <- new Array(7,7,7)  
    %v[0][1][3] <- 1  
    return 0  
}
```

IR

```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
      var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
      call callee ( args? ) | var <- call callee ( args? ) |
      var <- new Array(args) | var <- new Tuple(t) ←
```

```
T ::= type | void
```

```
type ::= int64([])* | tuple | code
```

Implicit initialization to "1"

```
callee ::= u | print | input | tensor-error
```

```
args ::= t | t ( , t)*
```

```
s ::= t | label | l
```

```
t ::= var | N
```

```
u ::= var | l
```

```
N ::= (+|-)? [0-9]+
```

```
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
```

```
l ::= @name
```

```
label ::= :name
```

```
var ::= %name
```

```
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

```
define int64 @myF (int64 %p1){
  :myLabel
  tuple %t
  %t <- new Tuple(7)
  %t[0] <- 3
  return 0
}
```


IR makes the CFG explicit

IR also makes complex data types explicit

- Explicit data types
- Explicit allocations
- Explicit access to size objects
 - E.g., length of an array

IR

```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
    var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
    call callee ( args? ) | var <- call callee ( args? ) |
    var <- new Array(args) | var <- new Tuple(t)
T ::= type | void
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l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

```
define int64 @myF (int64 %p1){
    :myLabel
    int64[][][] %v
    int64 %l_0
    int64 %l_1
    int64 %l_2
    %v <- new Array(7,7,7)
    %l_0 <- length %v 0
    %l_1 <- length %v 1
    %l_2 <- length %v 2
    return 0
}
```

IR

```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
      var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
      call callee ( args? ) | var <- call callee ( args? ) |
      var <- new Array(args) | var <- new Tuple(t)
T ::= type | void
type ::= int64([])* | tuple | code
callee ::= u | print | input | tensor-error
args ::= t | t ( , t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]+
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

```
define int64 @myF (int64 %p1){
  :myLabel
  tuple %v
  int64 %l
  %v <- new Tuple(7)
  %l <- length %v
  return 0
}
```

IR makes the CFG explicit


IR also makes complex data types explicit

- Explicit data types
- Explicit allocations
- Explicit access to size objects
 - E.g., length of an array
- Object accesses only possible in simple assignments

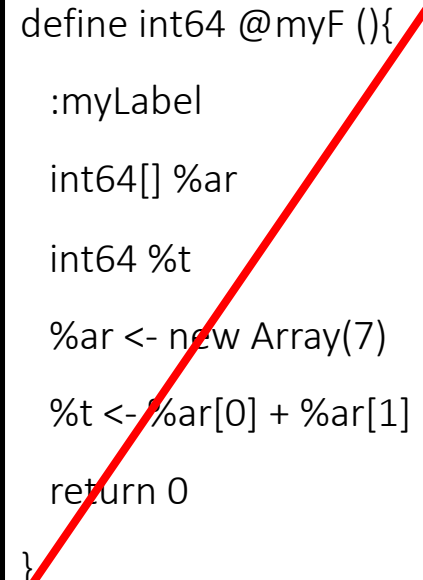
IR

```
p ::= f+
f ::= define T l ( (type var)* ) { bb+ }
bb ::= label i * te
te ::= br label | br t label label | return | return t
i ::= type var | var <- s | var <- t op t |
    var <- var([t])+ | var([t])+ <- s | var <- length var t | var <- length var |
    call callee ( args? ) | var <- call callee ( args? ) |
    var <- new Array(args) | var <- new Tuple(t)
T ::= type | void
type ::= int64([])* | tuple | code
callee ::= u | print | input | tensor-error
args ::= t | t ( , t)*
s ::= t | label | l
t ::= var | N
u ::= var | l
N ::= (+|-)? [0-9]+
op ::= + | - | * | & | << | >> | < | <= | = | >= | >
l ::= @name
label ::= :name
var ::= %name
name ::= sequence of chars matching [a-zA-Z_][a-zA-Z_0-9]*
```

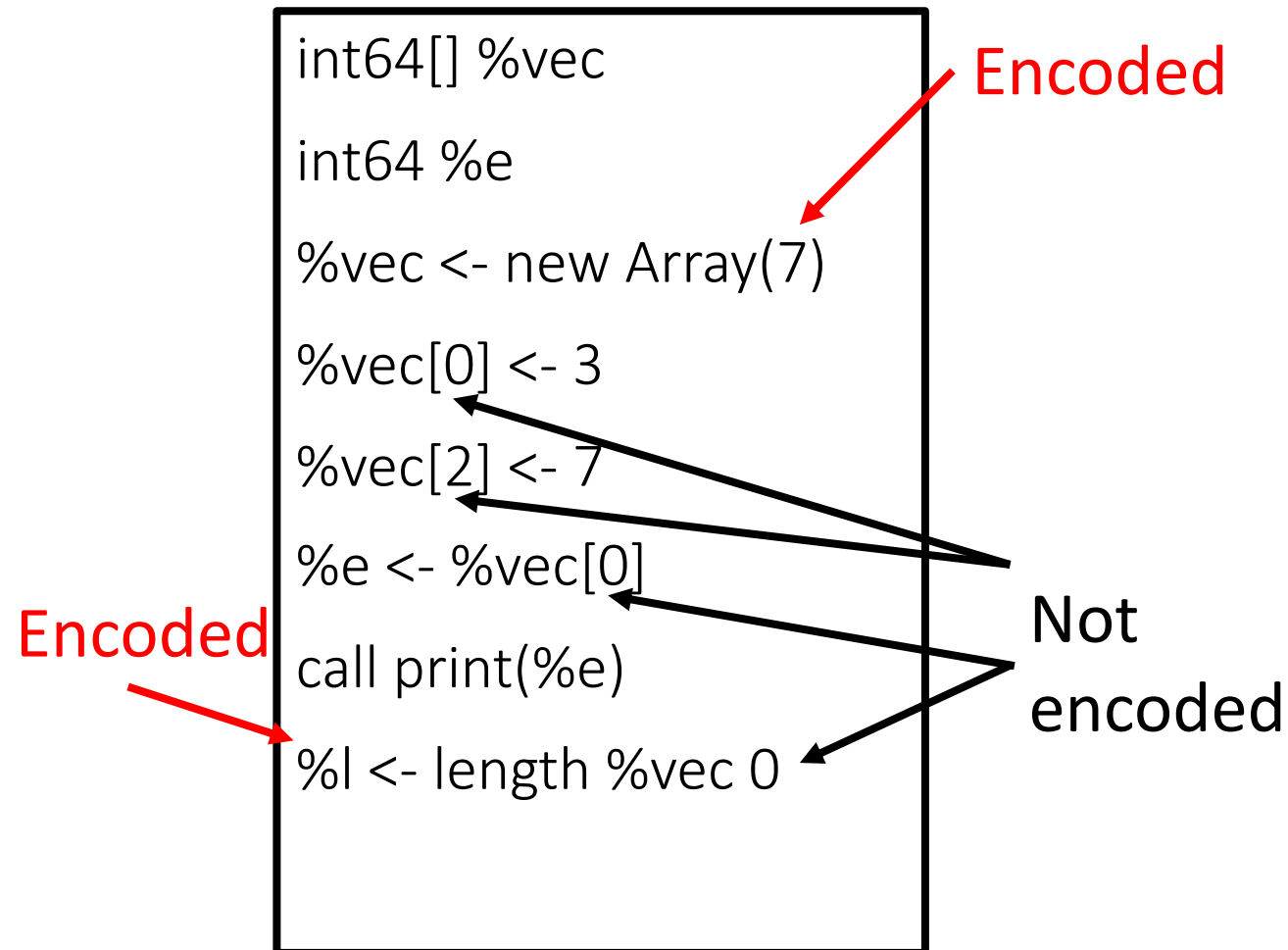
```
define int64 @myF (){
  :myLabel
  int64[] %ar
  int64 %v0
  int64 %v1
  int64 %t
  %ar <- new Array(7)
  %v0 <- %ar[0]
  %v1 <- %ar[1]
  %t <- %v0 + %v1
  return 0
}
```



```
define int64 @myF (){
  :myLabel
  int64[] %ar
  int64 %t
  %ar <- new Array(7)
  %t <- %ar[0] + %ar[1]
  return 0
}
```



Indices of array and tuple accesses are not encoded



Indices and dimension# in length are not encoded

- Accessing length of a dimension

```
%l <- length %ar %dimID
```

- Accessing length of a tuple

```
%l <- length %tuplePtr
```

- Accessing array element

```
%ar[%e1][%e2] <- %v1
```

```
%v2 <- %ar[%e1][%e2]
```

- Allocating an array

```
%ar <- new Array(%dim1, %dim2)
```

Encoded

Not encoded

Variable definition

- The code must define (statically) a variable before using it
- All variable definitions must appear in the function before all of its uses and at the entry point basic block



```
int64 %d  
%d <- 5
```

```
%d <- 5  
int64 %d
```

```
:E  
br :S  
:S  
int64 %d  
%d <- 5  
return
```


Final notes on IR

Same undefined behaviors as for L3
but without the one related to the last instruction of a function

L3

```
define @myF (%p1){  
  %p2 <- %p1 + 1  
}
```

IR

```
define void @myF (int64 %p1){  
  int64 %p2  
  %p2 <- %p1 + 1  
  return  
}
```

Now that you know the IR language

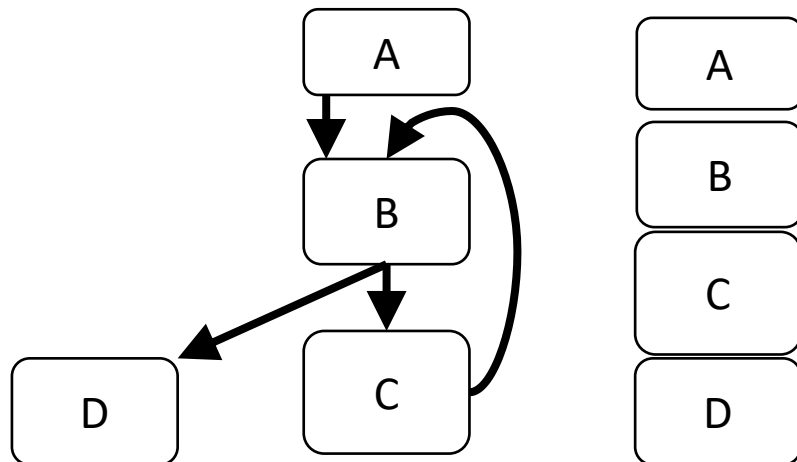
Rewrite all of your L3 programs in IR

Outline

- IR
- Linearize the CFG
- Linearize the data types

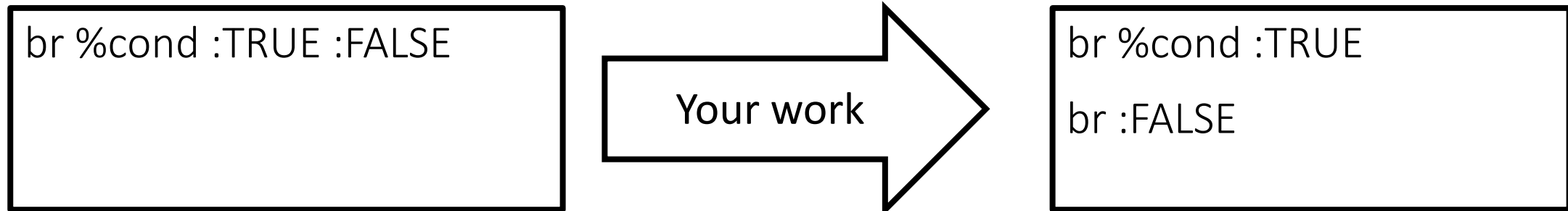
From CFG to a sequence of instructions

- CFG is a 2-dimension representation
- L3 is a 1-dimension representation
- We need to linearize CFG to generate L3
- Any order will preserve the original semantics as long as the entry point BB is the first one (property of the CFG)



Naïve solution (not ok for your homework)

- Ignore the problem
- In other words:
the sequence of basic blocks described in the IR program file
is going to be the sequence chosen
- Translate a two labels IR branch into 2 branches in L3

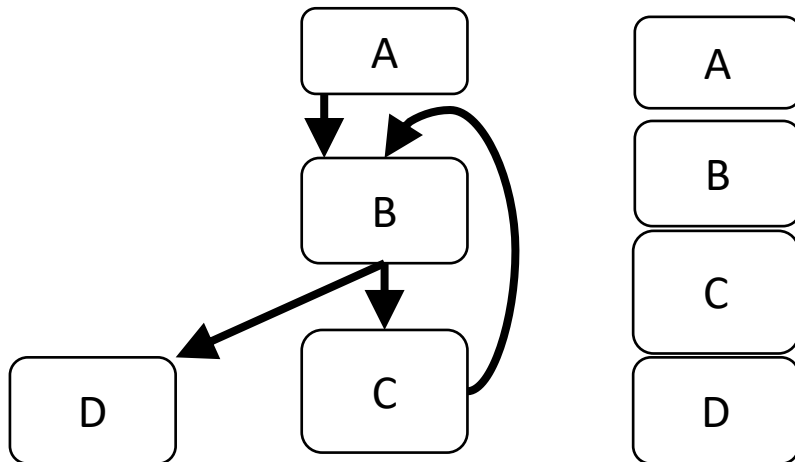


From CFG to a sequence of instructions

- CFG is a 2-dimension representation
- L3 is a 1-dimension representation
- We need to linearize CFG to generate L3
- Any order will preserve the original semantics as long as the entry point BB is the first one (property of the CFG)
- Different orders will have a different #branches
- We want to select the one with the lowest #branches
 - Run-time vs. compile-time

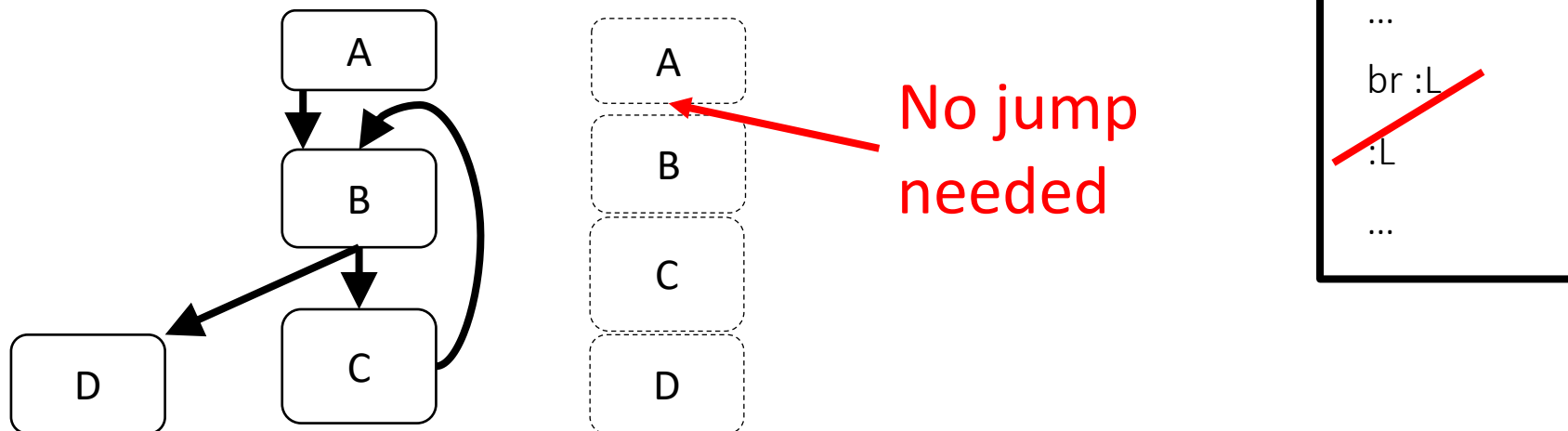
From CFG to a sequence of instructions

- CFG is a 2-dimension representation
- L3 is a 1-dimension representation
- We need to linearize CFG to generate L3



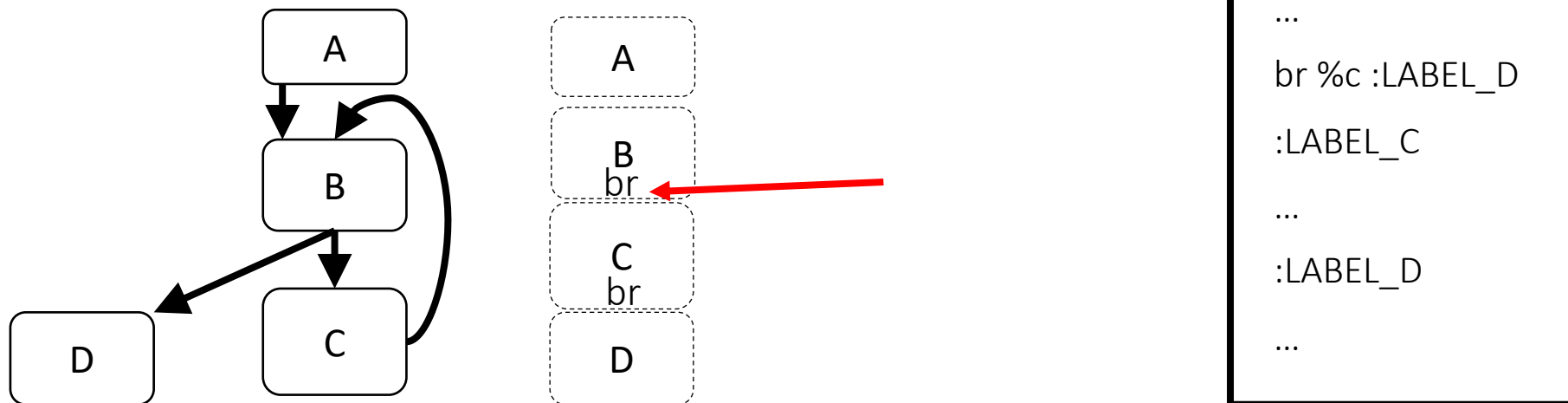
From CFG to a sequence of instructions

- CFG is a 2-dimension representation
- L3 is a 1-dimension representation
- We need to linearize CFG to generate L3



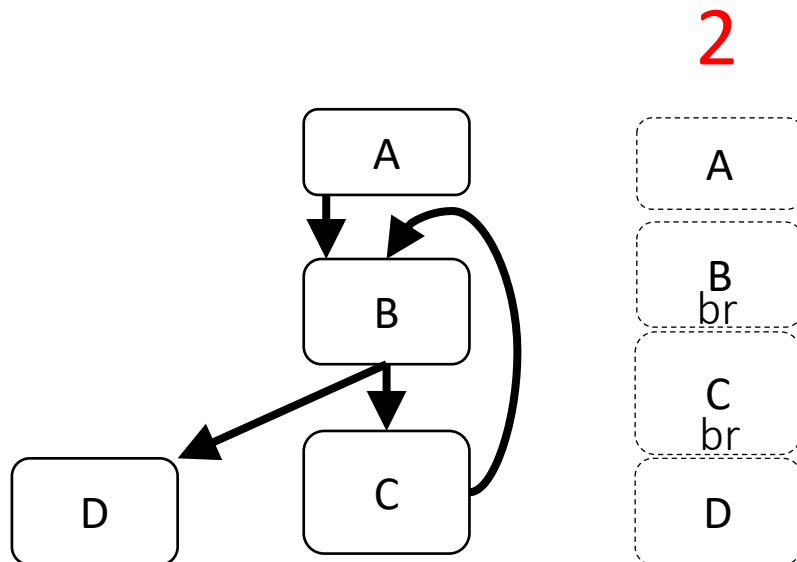
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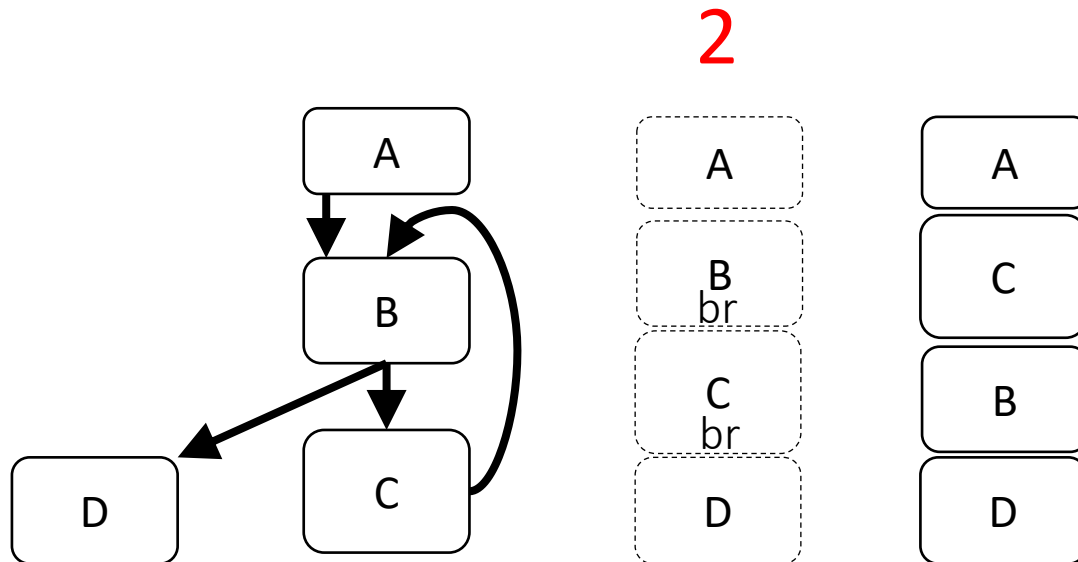
Let us assume the loop B-C is executed many times.

How many branches do we execute per loop iteration?

Is this the best we can do?

From CFG to a sequence of instructions

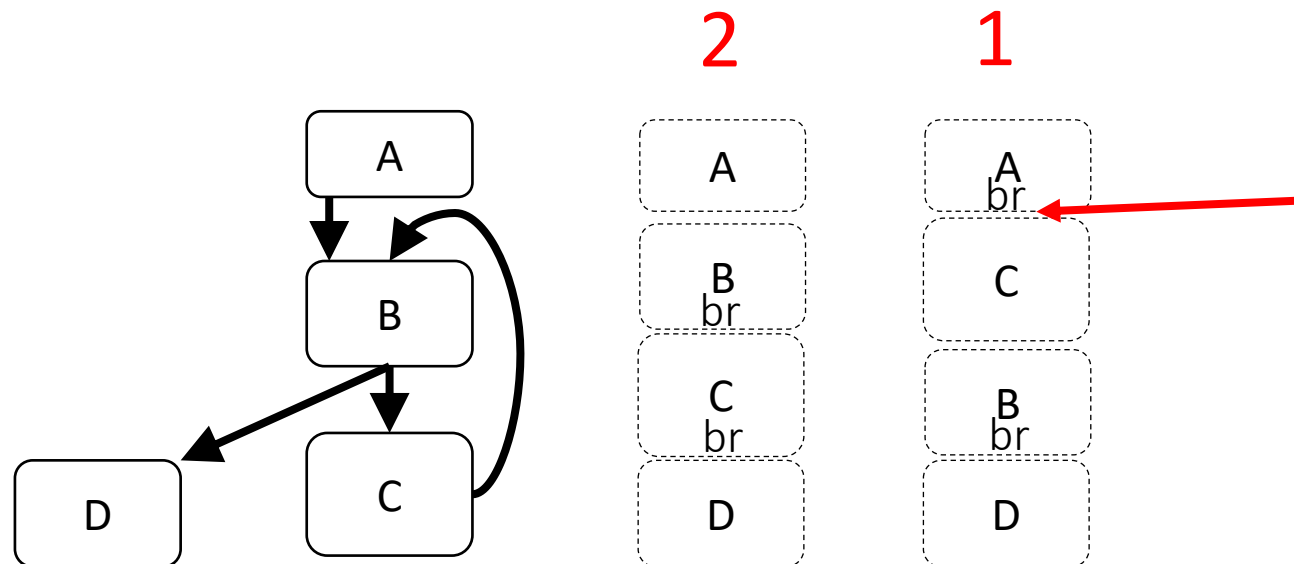
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From CFG to a sequence of instructions

- CFG is a 2-dimension representation
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How many branches do we execute per loop iteration?



The tracing problem

CFG linearization

- A trace is a sequence of basic blocks (instructions) that could be executed at run time
 - It can include conditional branches
- A program has many overlapping traces
- For our goal:
 - Find a set of traces that cover the whole function without any overlapping
 - Each basic block belongs to exactly 1 trace
 - Remove unconditional branches within the same trace

Finding the not overlapping traces

```
list <- all basic blocks
```

```
do{
```

```
  tr = new trace()
```

```
  bb = fetch_and_remove(list)
```

```
  while (bb is not marked){
```

```
    mark bb
```

```
    tr.append(bb)
```

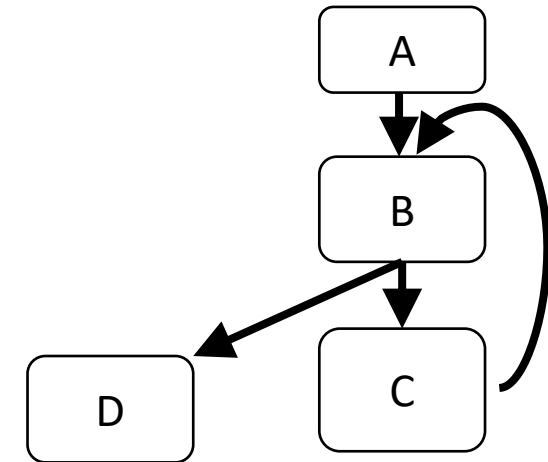
```
    succs = successors(bb)
```

```
    if there is  $c \in \text{succs}$  such that  $c$  is unmarked and profitable(bb, c)
```

```
      bb = c
```

```
  }
```

```
} while (list is not empty)
```



Outline

- IR
- Linearize the CFG
- Linearize the data types

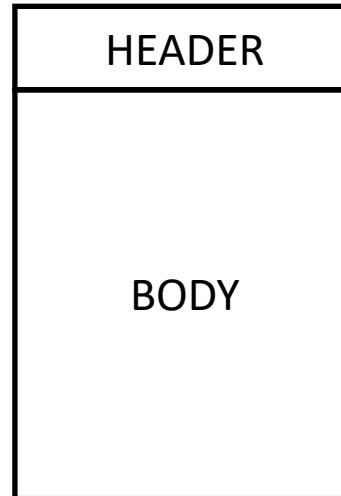
IR features

- Basic blocks and control Flow Graph (CFG)
- Data types
 - Multi dimension arrays

```
define int64 @myF (int64 %p1){  
  :myLabel  
  int64 %p2  
  %p2 <- %p1 + 1  
  return %p2  
}
```


Multi-dimension arrays

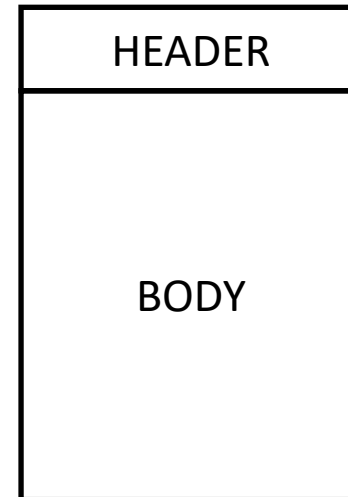
- The IR compiler must linearize all arrays
 - Data layout
 - Body
- The IR compiler must store the dimension lengths
 - Data layout
 - Header



```
int64[][] %m
int64 %e
int64 %l0
int64 %l1
%m <- new Array(7,7)
%m[0][0] <- 3
%m[2][1] <- 7
%e <- %m[0][0]
call print(%e)
%l0 <- length %m 0
%l1 <- length %m 1
```

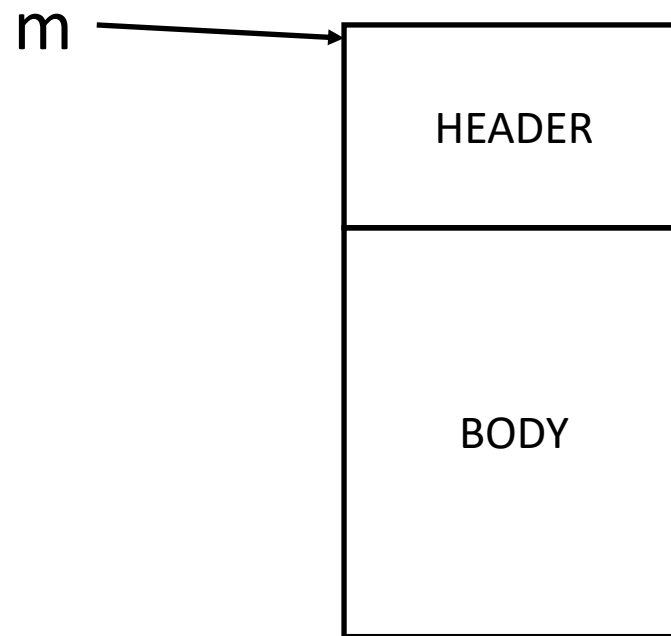
Data layout for multi-dimension arrays

```
int64[][] %m  
%m <- new Array(7,9)
```



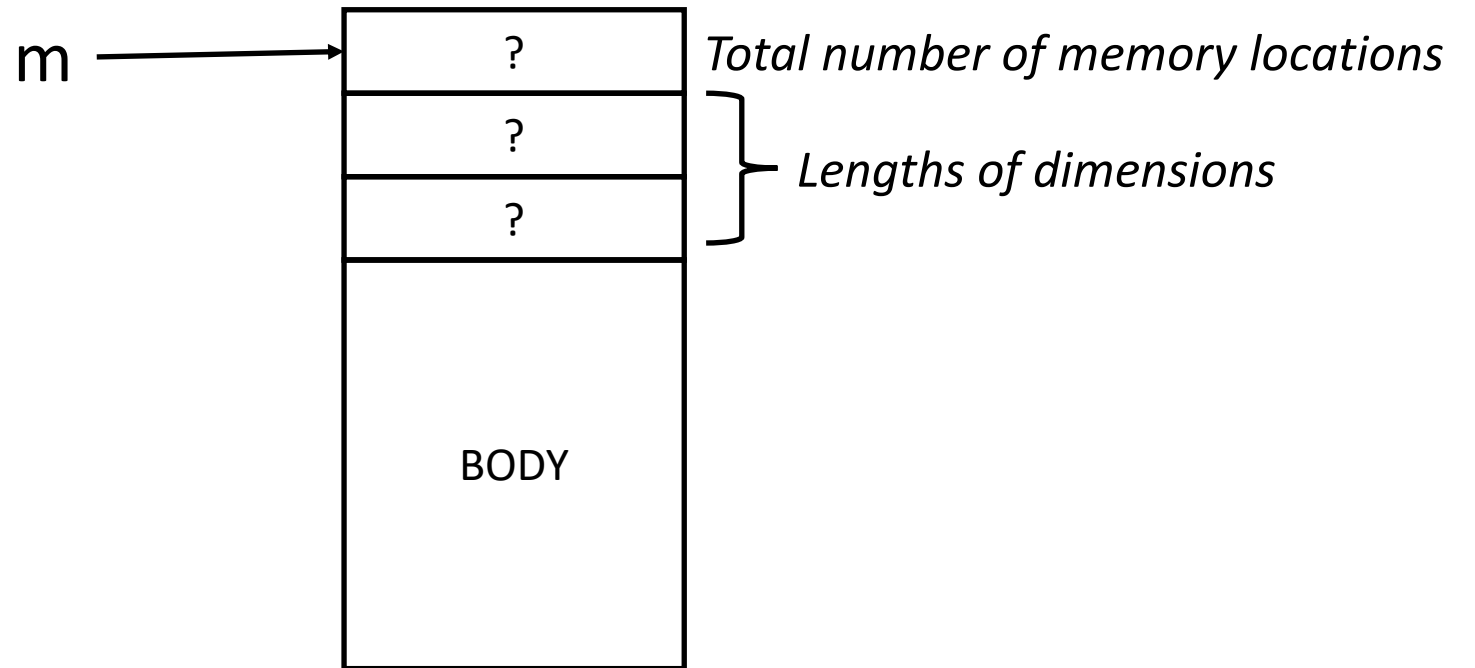
Data layout for multi-dimension arrays

```
int64[][] %m  
%m <- new Array(7,9)
```



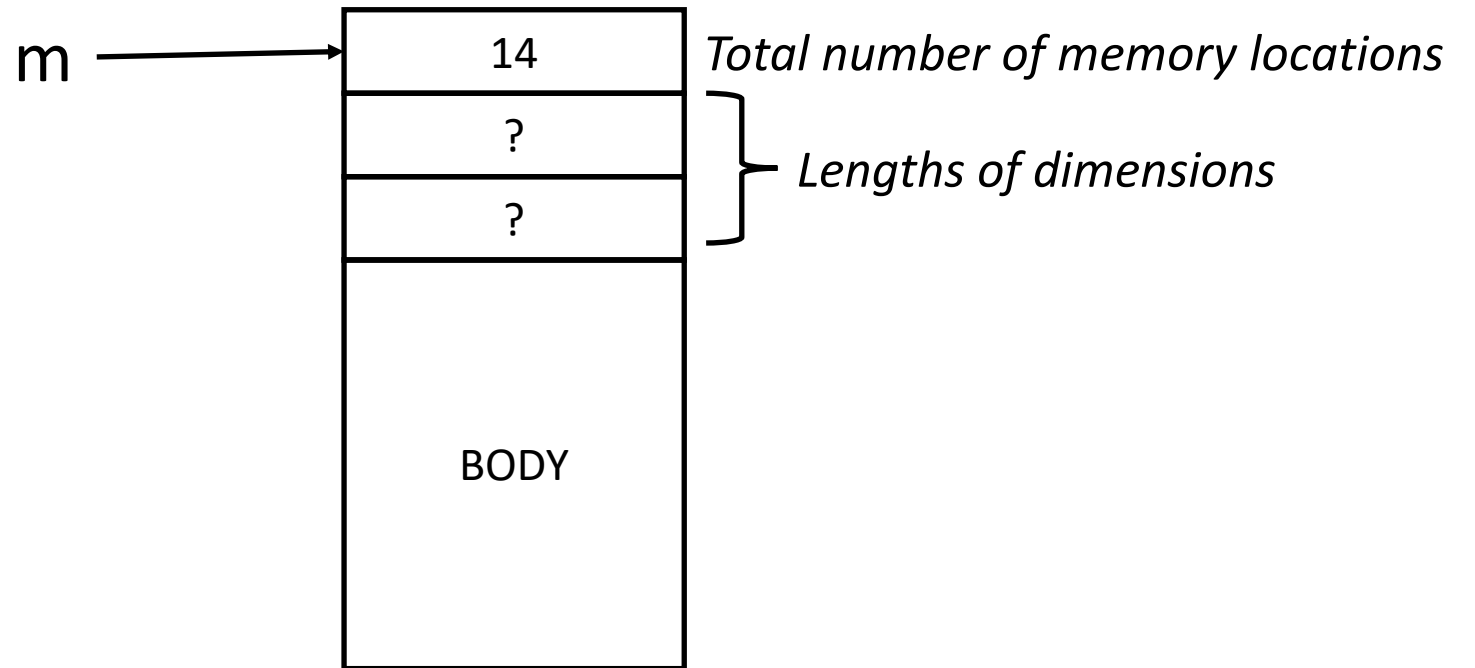
Data layout for multi-dimension arrays

```
int64[][] %m
%m <- new Array(7,9)
```



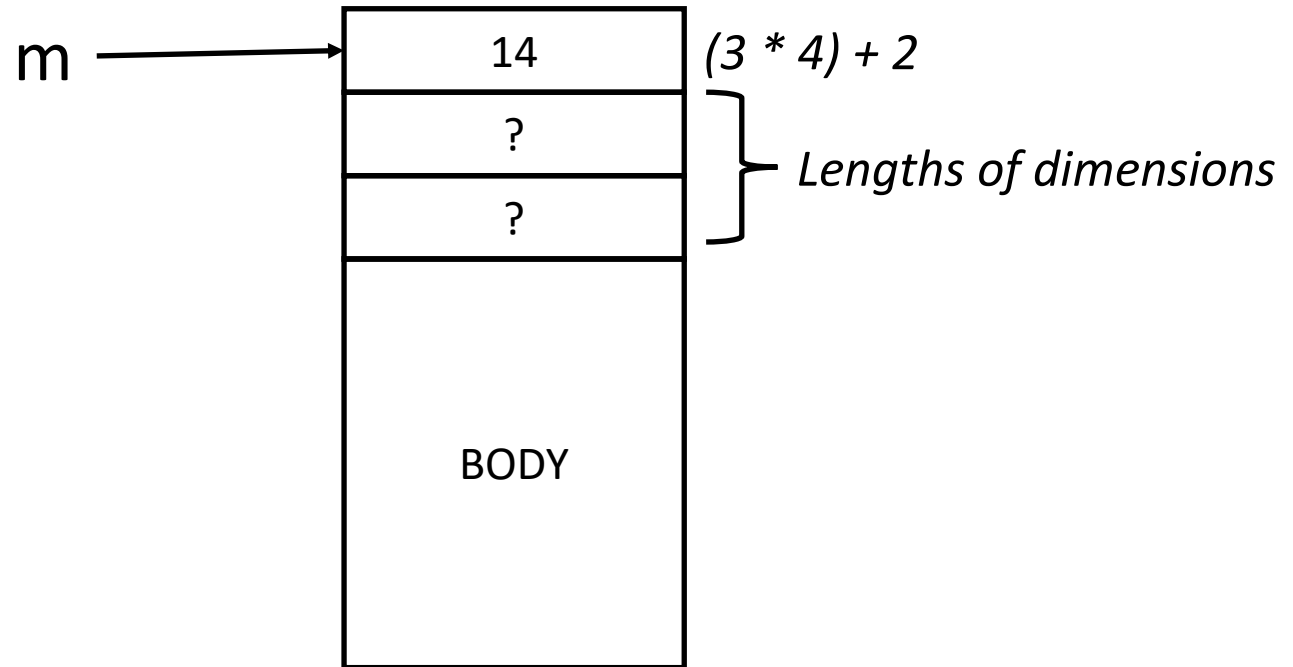
Data layout for multi-dimension arrays

```
int64[][] %m
%m <- new Array(7,9)
```



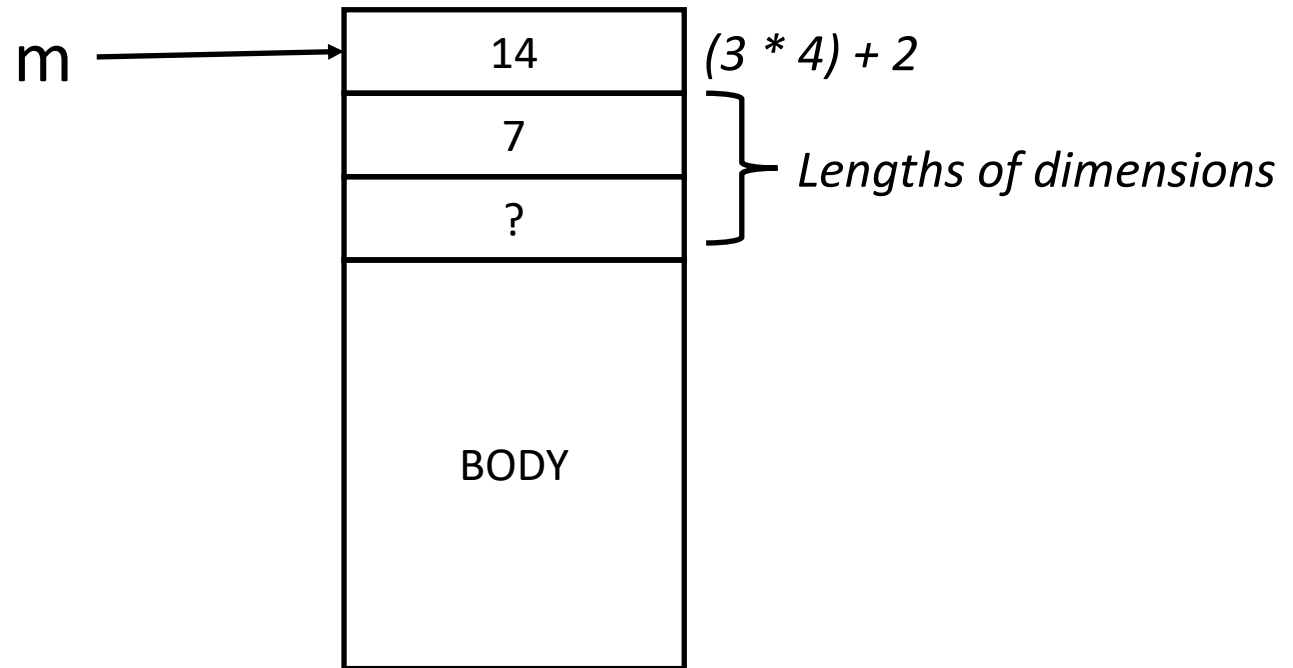
Data layout for multi-dimension arrays

```
int64[][] %m
%m <- new Array(7,9)
```



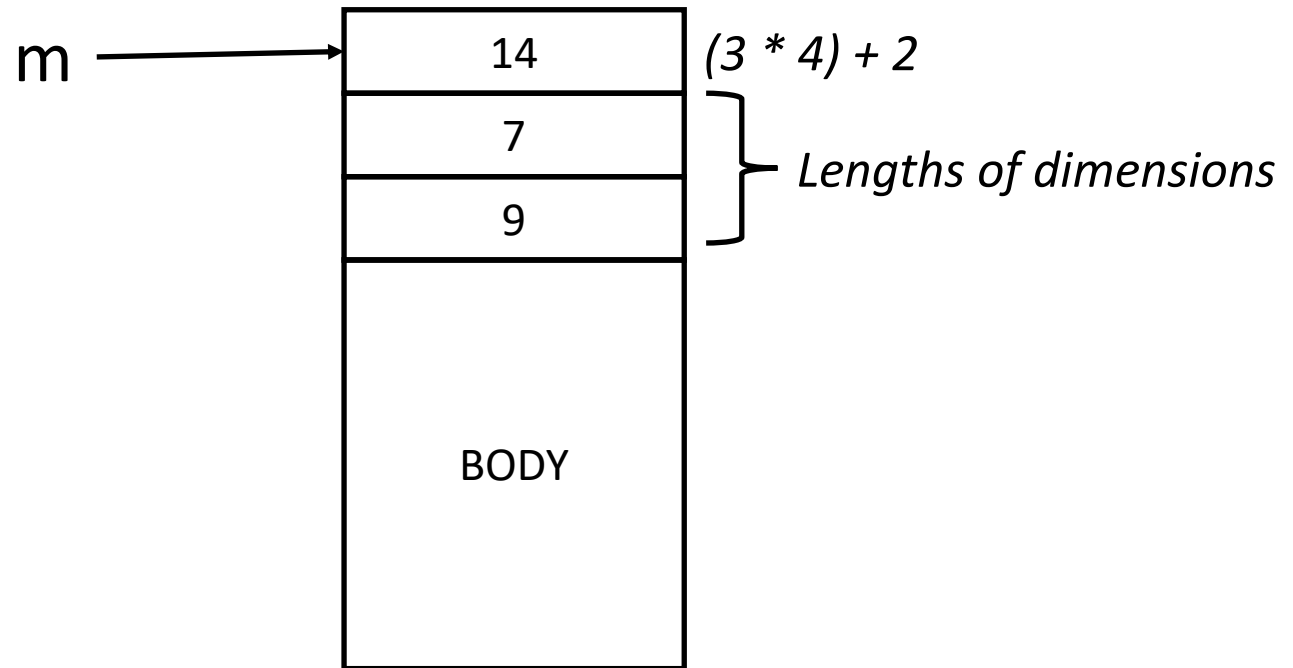
Data layout for multi-dimension arrays

```
int64[][] %m  
%m <- new Array(7,9)
```

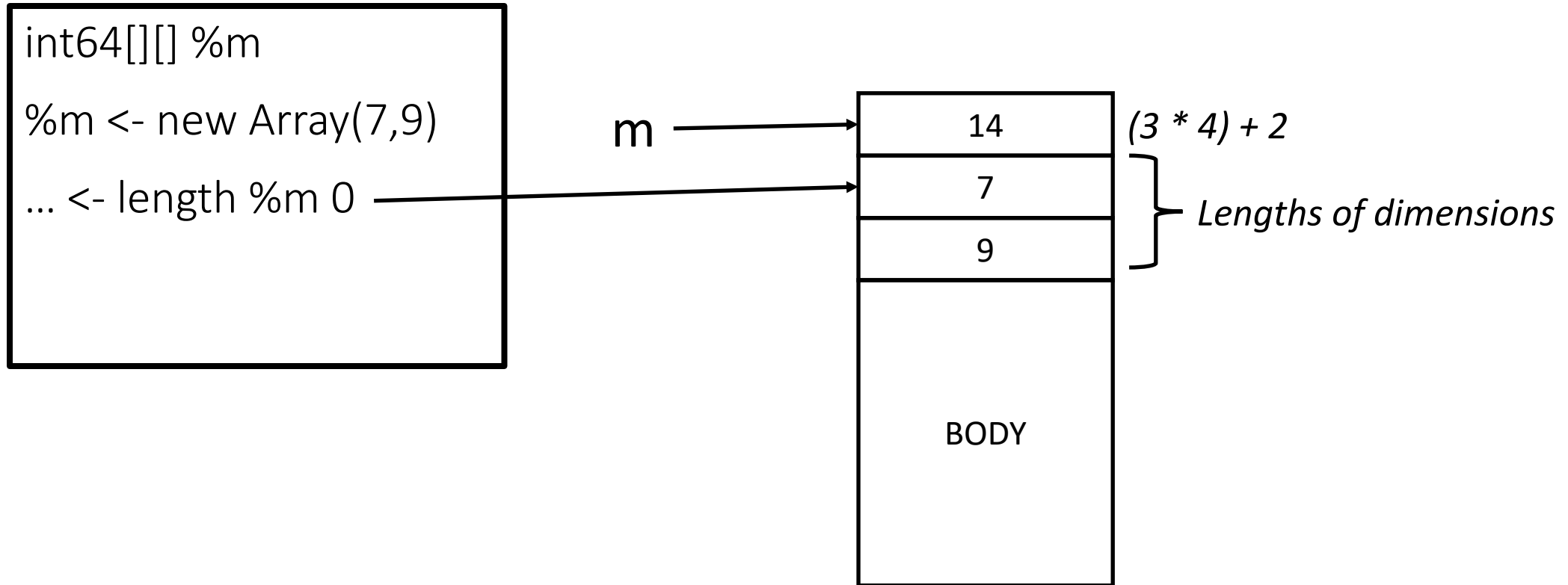


Data layout for multi-dimension arrays

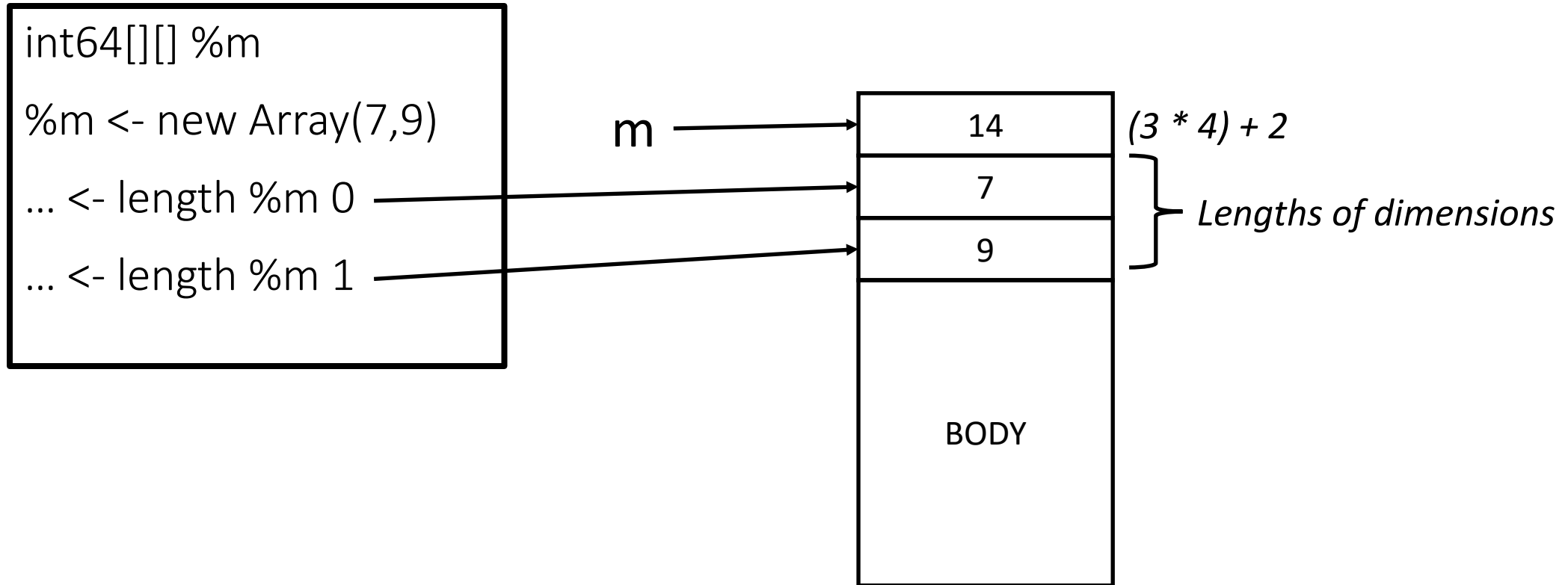
```
int64[][] %m
%m <- new Array(7,9)
```



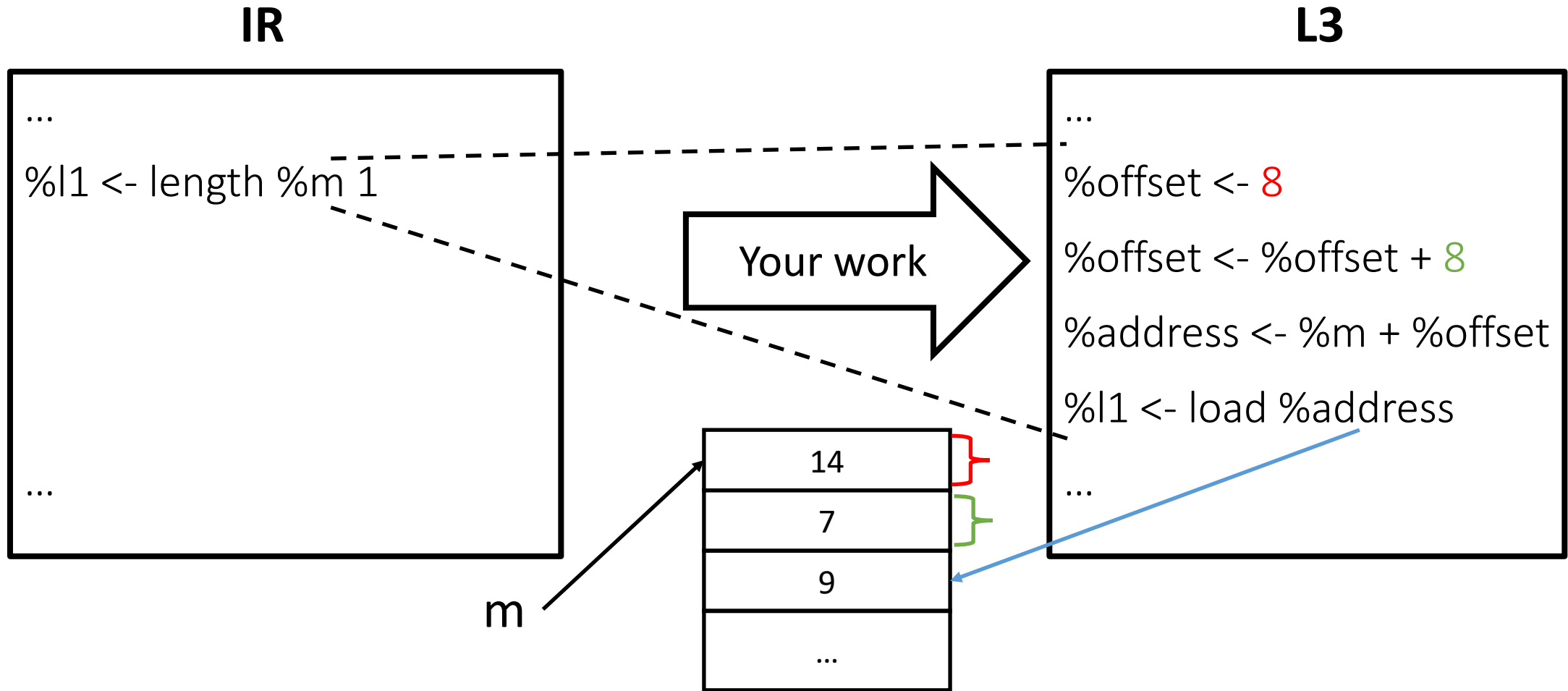
Data layout for multi-dimension arrays



Data layout for multi-dimension arrays



Translating length for arrays



Translating new Array()

Computing the number of memory locations

Your work

| |
|-------------|
| arrayLength |
| %p1 |
| %p2 |
| ... |

```
...  
Int64[][] %a  
%a <- new Array(%p1,%p2)
```

```
...  
%p1D <- %p1 >> 1  
%p2D <- %p2 >> 1  
%v0 <- %p1D * %p2D  
%v0 <- %v0 + 2
```

Why 2?

```
%v0 <- %v0 << 1  
%v0 <- %v0 + 1
```

Encoding

```
%a <- call allocate(%v0, 1)  
%v2 <- %a + 8  
store %v2 <- %p1  
%v3 <- %a + 16  
store %v3 <- %p2  
...
```

Linearize an array

- `m[0][0]`

```
%o1 <- 8
```

```
%o2 <- 2 * 8
```

```
%o <- %o1 + %o2
```

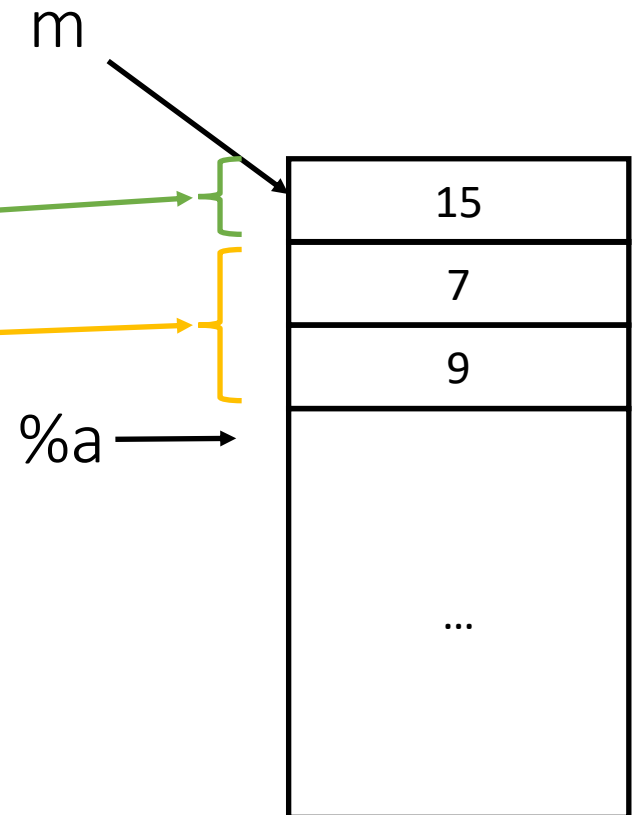
```
%a <- %m + %o
```

```
store %a <- ...
```

- `m[0][1]?`

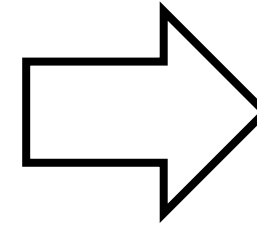
- By row, by column

```
int64[][] %m  
%m <- new Array(7,9)  
%m[0][0] <- ...
```



Data layout for this class

| | | | |
|-----|-----|-----|-----|
| 0,0 | 0,1 | 0,2 | 0,3 |
| 1,0 | 1,1 | 1,2 | 1,3 |



| |
|-----|
| 0,0 |
| 0,1 |
| 0,2 |
| 0,3 |
| 1,0 |
| 1,1 |
| 1,2 |
| 1,3 |

- Matrix M x N
 - Offset for all: $B = 8 + (2 * 8)$
 - Offset A[0][1] = $B + (1) * 8$
 - Offset A[0][2] = $B + (2) * 8$
 - Offset A[0][i] = $B + (i) * 8$
 - Offset A[1][0] = $B + (1 * N) + 0) * 8$
 - Offset A[i][j] = $B + (i * N) + j) * 8$
- Tensor L x M x N: $B = 8 + (3 * 8)$
 - Offset A[k][i][j] = $B + ((k * M * N) + (i * N) + j) * 8$

Linearization example (2)

IR: L x M x N: %A[%k][%i][%j] <- 5

L3: $\text{Offset} = 8 + (3 * 8) + ((k * M * N) + (i * N) + j) * 8$

- ADDR_M <- A + 16
- M_ <- load ADDR_M
- M <- M_ >> 1
- ADDR_N <- A + 24
- N_ <- load ADDR_N
- N <- N_ >> 1
- newVar1 <- i * N
- M_N <- M * N
- newVar2 <- k * M_N
- newVar3 <- newVar2 + newVar1
- index <- newVar3 + j
- offsetInBody <- index * 8
- offset <- offsetInBody + 32
- addr <- A + offset
- store addr <- 5

To fetch M

To fetch N

// newVar1 <- (i * N)

// newVar2 <- (k * M * N)

// newVar3 <- (k * M * N) + (i * N)

// index <- (k * M * N) + (i * N) + j

// 8 + (3 * 8)

Multi-dimension arrays

- No limit to the number of dimensions

```
int64[][] %m  
%m <- new Array(7,9)  
Int64[][][][][][][][] %crazy  
%crazy <- new Array(7,7,7,7,7,7,7,7,7,7)
```

- The data layout follows the scheme of the previous slides

IR features

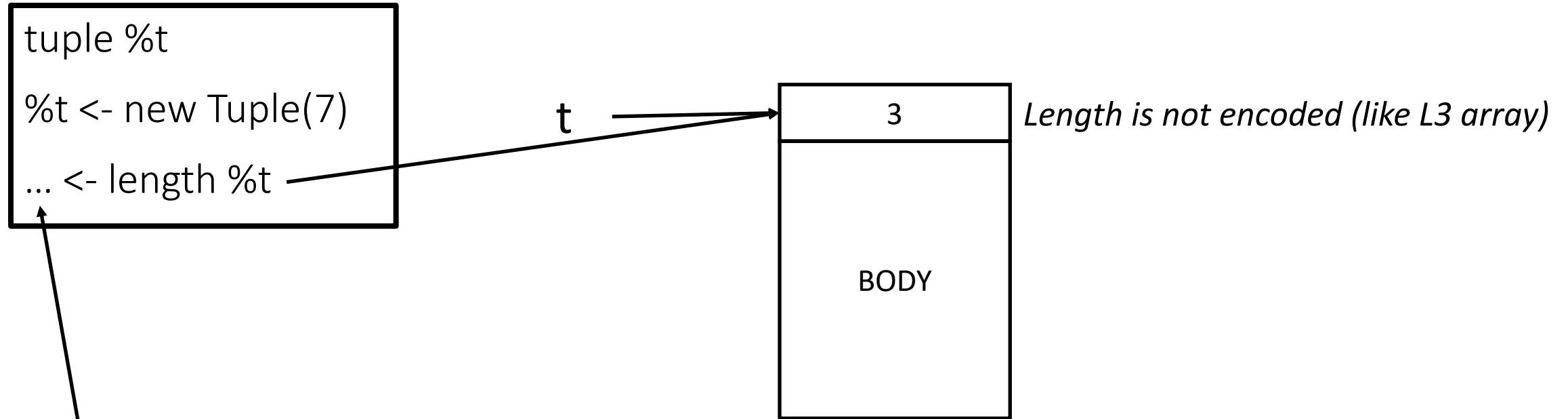
- Basic blocks and control Flow Graph (CFG)
- Data types
 - Multi dimension arrays
 - Tuples

Tuples

- An IR tuple is an heterogeneous 1-dimension array
- So, an IR tuple is equivalent to an L3 array

```
tuple %t
%t <- new Tuple(7)
%t[0] <- 5
int64[] %a
%a1 <- new Array(3)
%t[1] <- %a1
%a2 <- new Array(5,3)
%t[2] <- %a2
```

Data layout for tuples



- Returned length is encoded
- The translation of “length” needs to encode the value loaded from memory

Translating tuples

```
...  
tuple %t  
%t <- new Tuple(7)  
-----  
%t[0] <- 5  
-----  
%v <- %t[0]  
...
```

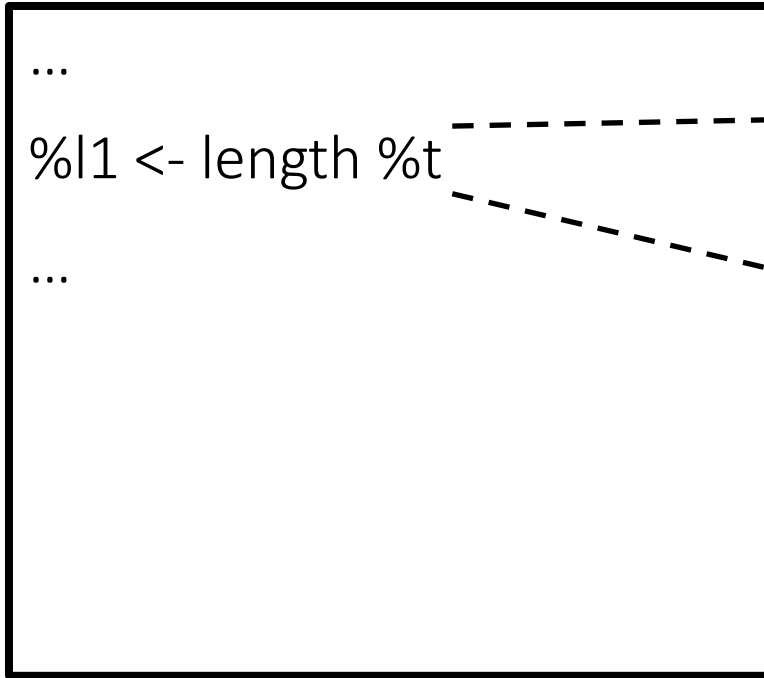
Your work



```
...  
%t <- call allocate(7, 1)  
-----  
%newVar0 <- %t + 8  
store %newVar0 <- 5  
-----  
%newVar1 <- %t + 8  
%v <- load %newVar1  
...
```

Translating length for tuples

IR

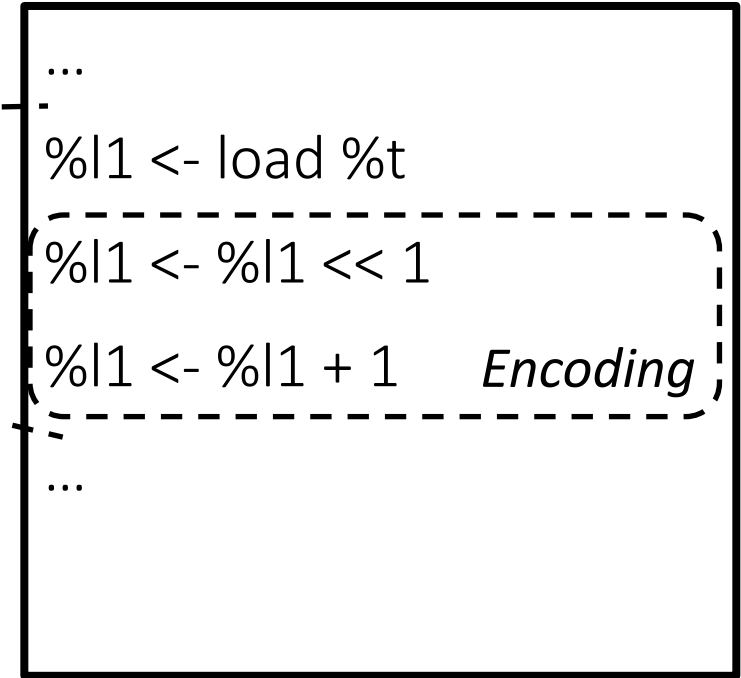


t

Your work

A large, hollow arrow pointing from the IR code block to the L3 code block, with the text "Your work" centered inside it.

L3



IR features

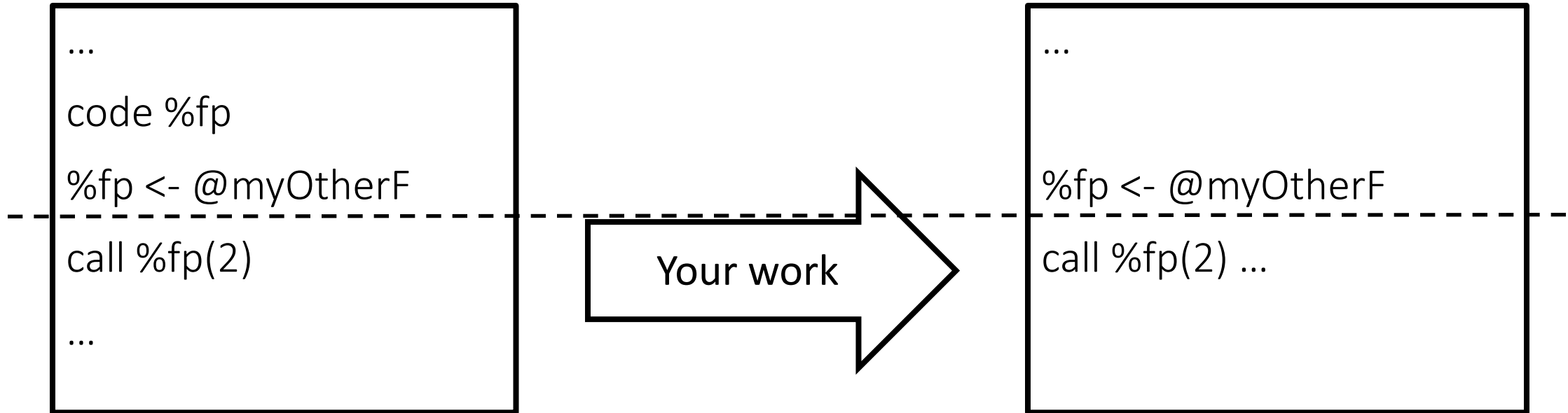
- Basic blocks and control Flow Graph (CFG)
- Data types
 - Multi dimension arrays
 - Tuples
 - Function pointers

Function pointers

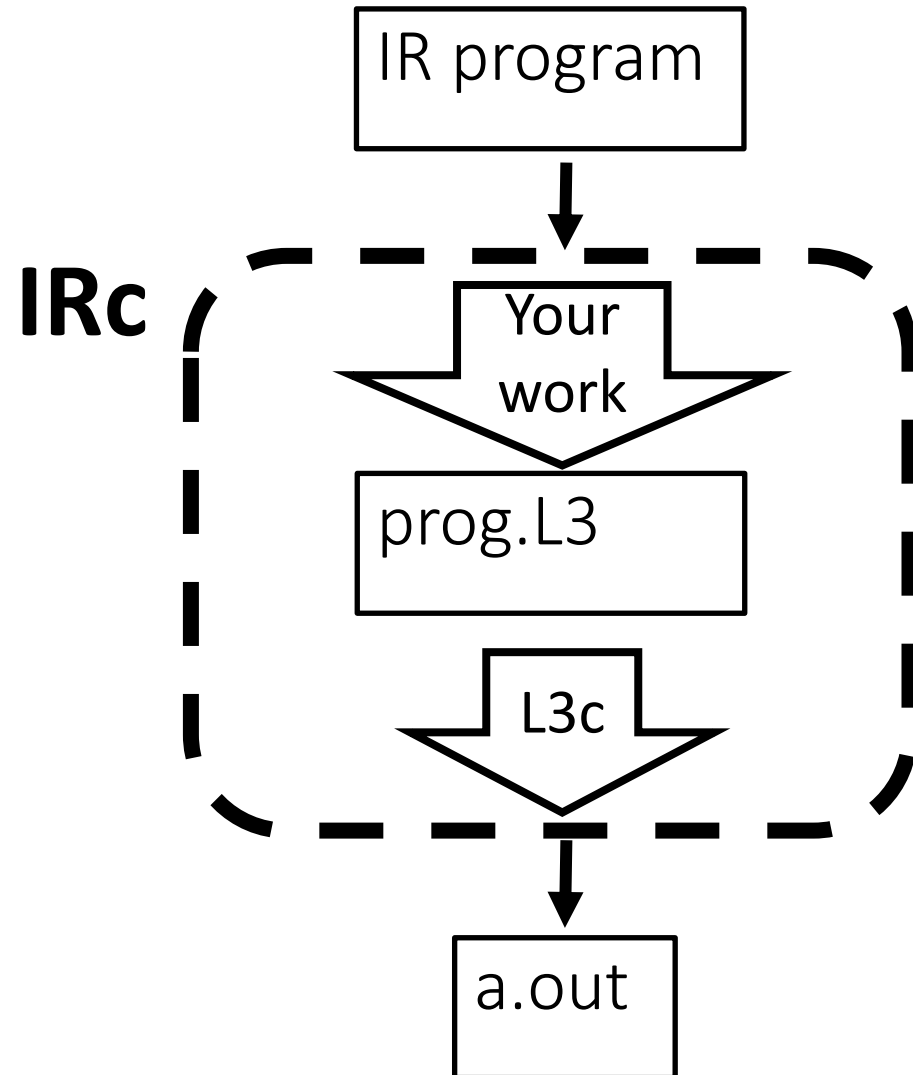
- Instances of type “code”
- Variables of type code can only store function names
- They can be used in call instructions
- They are normal variables
- They can be stored in tuples

```
define code @myF (tuple %t){  
  code %fp  
  %fp <- @myOtherF  
  call %fp (%firstArg,2)  
  %t[0] <- %fp  
  return %fp  
}
```

Translating function pointers



Homework #5: the IR compiler (IRc)



- To build IRc:
translate an IR program
to an equivalent L3
- We need to linearize the arrays
- We need to translate
the other IR instructions

Always have faith in your ability

Success will come your way eventually

Best of luck!