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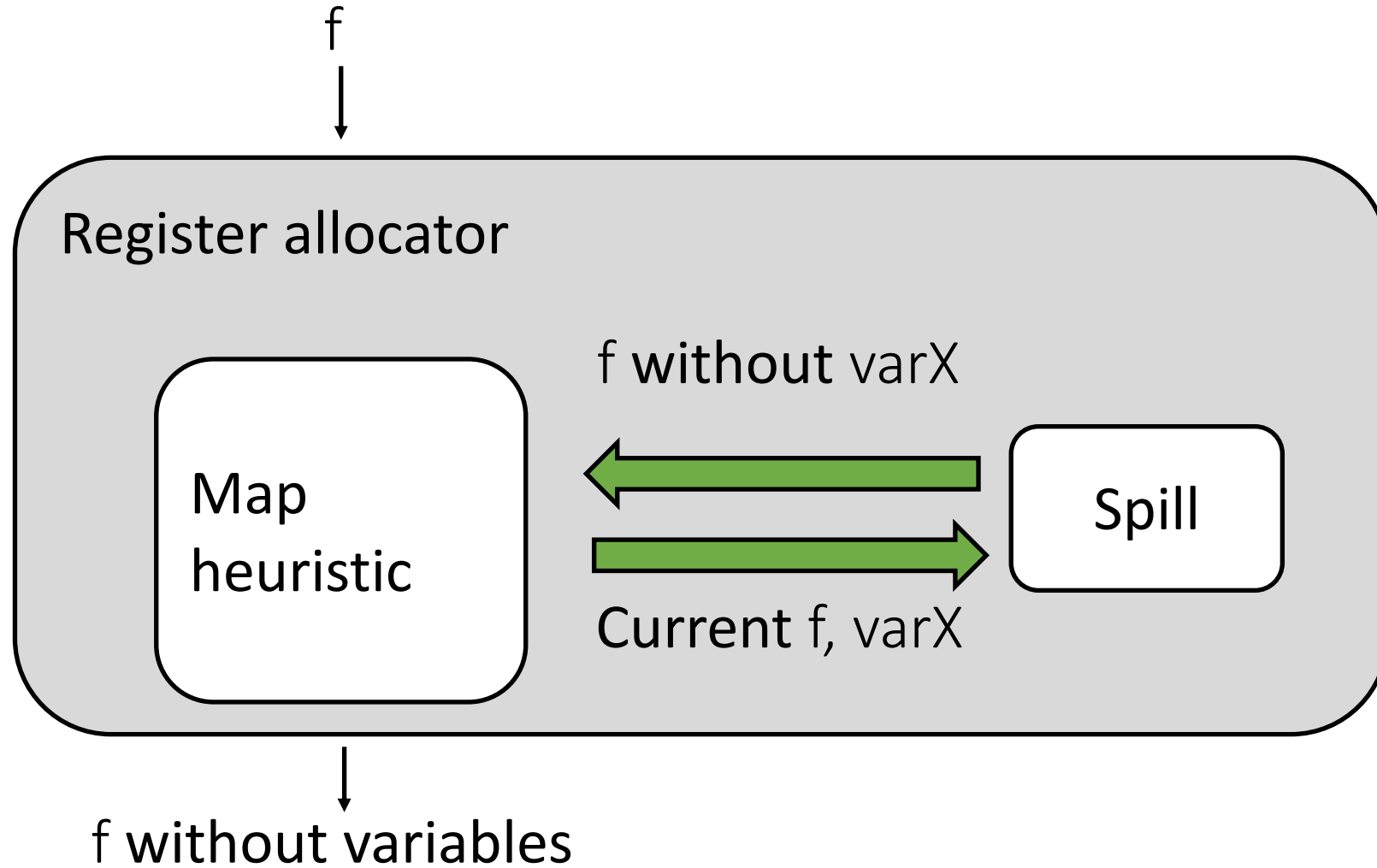
Liveness analysis



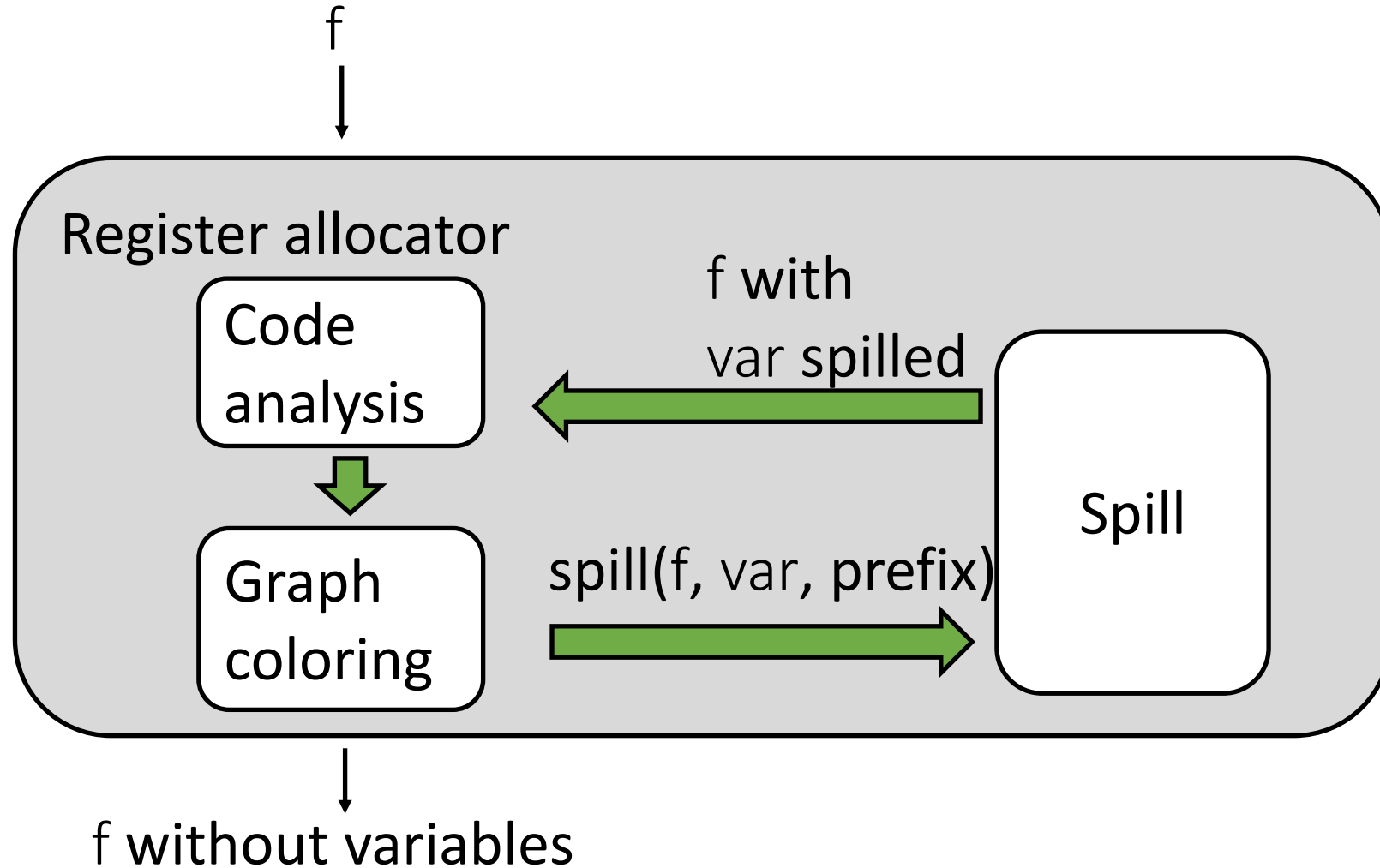
Outline

- Introduction to register allocation
- Liveness analysis
- Calling convention

A register allocator structure



A graph-coloring register allocator structure



Task: From Variables to Registers

```
(@MyVeryImportantFunction 0
```

```
%MyVar1 <- 2  
%MyVar2 <- 40  
%MyVar3 <- %MyVar1  
%MyVar3 += %MyVar2  
print %MyVar3  
)
```

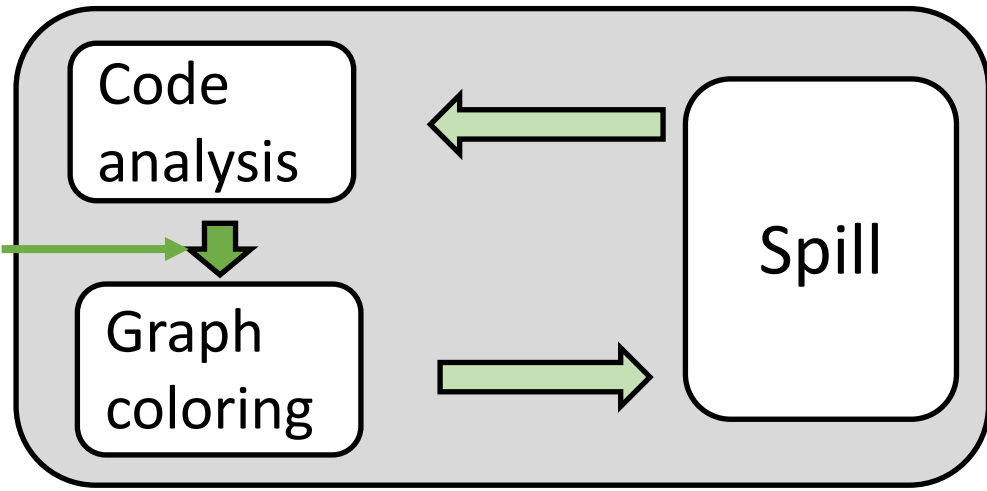


- Why can we map MyVar1 and MyVar3 to r8?
- Why can't we map MyVar1 and MyVar2 to r8? Software



Hardware

We built the interference graph
To compute it automatically,
we need the liveness analysis



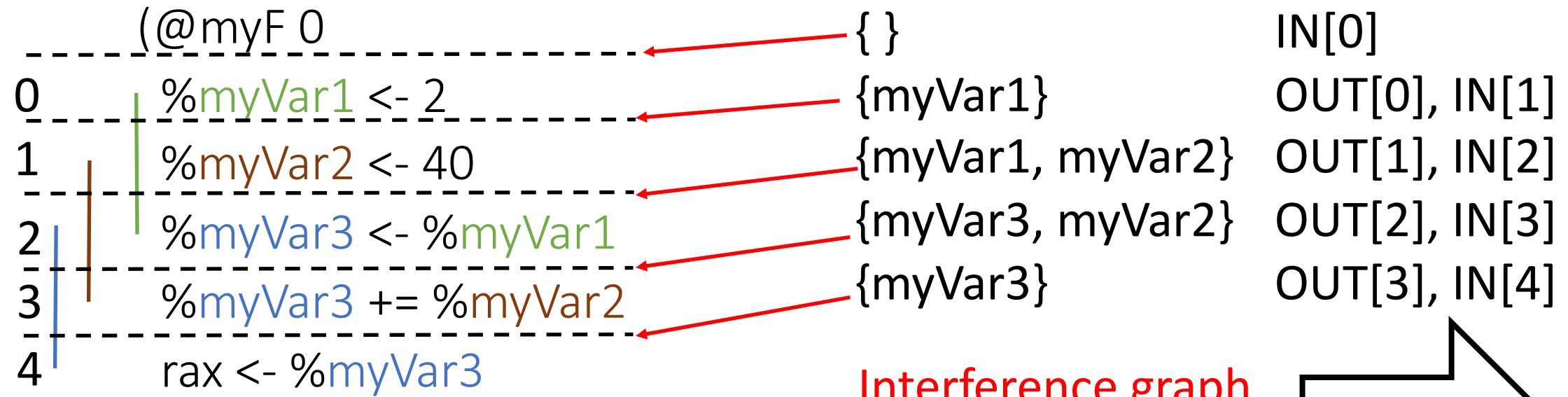
Liveness analysis

Goal:

Identify the variables whose values might be used in the future just before and just after a given instruction i ,

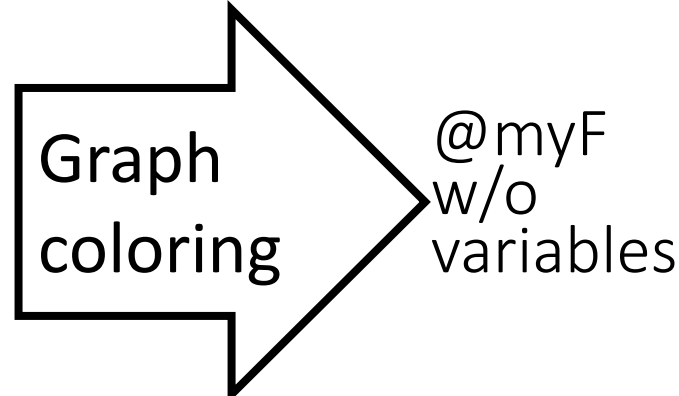
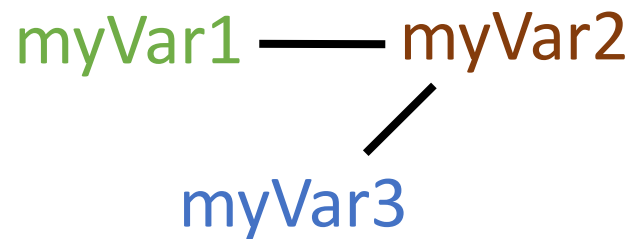
for every i in a function f

IN (just before) and OUT (just after) sets



return

Interference graph



Live ranges

Outline

- Introduction to register allocation
- Liveness analysis
- Calling convention

Variables in the liveness analysis

- General Purpose (GP) 64-bit registers are seen as variables for the liveness analysis
 - `rsp` is not included
- Every time we say “variable” in the context of liveness analysis, we mean either L2 variables or GP 64-bit registers
- IN and OUT sets of the liveness analysis includes variables
 - Hence, they include L2 variables or GP 64-bit registers
 - $IN[i] = \{r10\}$

Execution path

```
(@myF 0
```

```
rdi <- 5  
call print 1  
return
```

```
)
```

Let i be an instruction,
we need to identify the set of variables
with values that will be used
just before and just after i
along all possible execution paths that
include i

```
(@myF2 1
```

```
cjump rdi < 4 :true  
:useless_label  
rdi <- 5  
call print 1  
return
```

```
:true
```

```
rdi <- 7  
call print 1  
return
```

```
)
```

*It is a
predecessor of*

*It is a
successor of*

Successors of an instruction

```
i ::= w <- s | w <- mem x M | mem x M <- s | w <- stack-arg M |  
w aop t | w sop sx | w sop N | mem x M += t | mem x M -= t | w += mem x M | w -= mem x M |  
w <- t cmp t | cjump t cmp t label | label | goto label |  
return | call u N | call print 1 | call input 0 | call allocate 2 | call tensor-error F |  
w++ | w-- | w @ w w E
```

An instruction *i* that has only one successor *s* and *s* is the instruction stored just after *i*

```
rdi <- 5
```

```
call print 1
```

```
r10 <- rax < 5
```

Successors of an instruction (2)

$i ::= w \leftarrow s \mid w \leftarrow \text{mem } x \ M \mid \text{mem } x \ M \leftarrow s \mid w \leftarrow \text{stack-arg } M \mid$
 $w \text{ aop } t \mid w \text{ sop } sx \mid w \text{ sop } N \mid \text{mem } x \ M \ += t \mid \text{mem } x \ M \ -= t \mid w \ += \text{mem } x \ M \mid w \ -= \text{mem } x \ M \mid$
 $w \leftarrow t \text{ cmp } t \mid \text{cjump } t \text{ cmp } t \ \text{label} \mid \text{label} \mid \text{goto } \text{label} \mid$
 $\text{return} \mid \text{call } u \ N \mid \text{call print } 1 \mid \text{call input } 0 \mid \text{call allocate } 2 \mid \text{call tensor-error } F \mid$
 $w++ \mid w-- \mid w \ @ \ w \ w \ E$

An instruction i that has only one successor s but s is not necessarily the instruction stored just after i

```
goto :MY_LABEL_0
:MY_LABEL_0
```

```
goto :MY_LABEL_0
rdi <- 5
call print 1
:MY_LABEL_0
```

Successors of an instruction (3)

$i ::= w \leftarrow s \mid w \leftarrow \text{mem } x \ M \mid \text{mem } x \ M \leftarrow s \mid w \leftarrow \text{stack-arg } M \mid$
 $w \ \text{aop } t \mid w \ \text{sop } sx \mid w \ \text{sop } N \mid \text{mem } x \ M \ += t \mid \text{mem } x \ M \ -= t \mid w \ += \text{mem } x \ M \mid w \ -= \text{mem } x \ M \mid$
 $w \leftarrow t \ \text{cmp } t \mid \text{cjump } t \ \text{cmp } t \ \text{label} \mid \text{label} \mid \text{goto } \text{label} \mid$
 $\text{return} \mid \text{call } u \ N \mid \text{call print } 1 \mid \text{call input } 0 \mid \text{call allocate } 2 \mid \text{call tensor-error } F \mid$
 $w++ \mid w-- \mid w \ @ \ w \ w \ E$

An instruction i that has no successor

Successors of an instruction (4)

$i ::= w \leftarrow s \mid w \leftarrow \text{mem } x \ M \mid \text{mem } x \ M \leftarrow s \mid w \leftarrow \text{stack-arg } M \mid$
 $w \ \text{aop } t \mid w \ \text{sop } sx \mid w \ \text{sop } N \mid \text{mem } x \ M \ += t \mid \text{mem } x \ M \ -= t \mid w \ += \text{mem } x \ M \mid w \ -= \text{mem } x \ M \mid$
 $w \leftarrow t \ \text{cmp } t \mid \text{cjump } t \ \text{cmp } t \ \text{label} \mid \text{label} \mid \text{goto } \text{label} \mid$
 $\text{return} \mid \text{call } u \ N \mid \text{call print } 1 \mid \text{call input } 0 \mid \text{call allocate } 2 \mid \text{call tensor-error } F \mid$
 $w++ \mid w-- \mid w \ @ \ w \ w \ E$

An instruction i that has two successors

```
cjump rax < 5 :L1
rdi <- 1
rsi <- 3
:L1
```

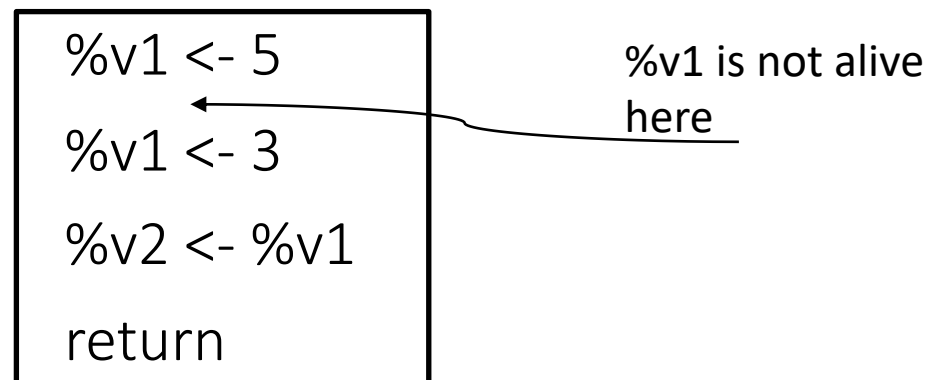
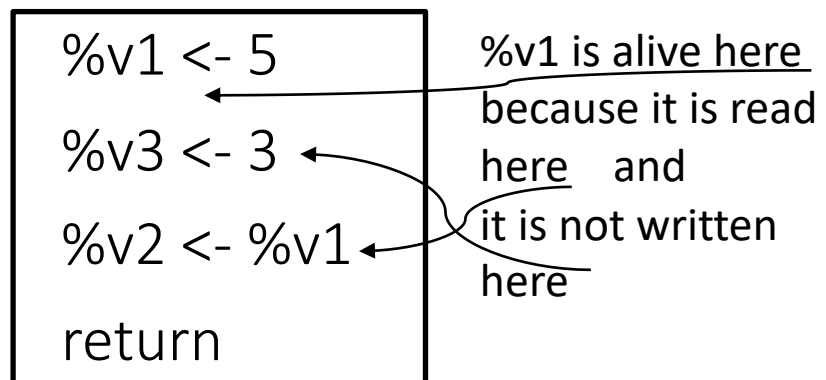
Now with knowledge about paths and successors
we can compute IN and OUT sets
of each instruction of a function
automatically

Liveness analysis

A variable is **alive** at a particular point in the program if its value at that point will be used in a path that starts from there (the future).

A variable is **dead** if it is not alive.

- To compute liveness at a given point, we need to look into the future
- A variable v is alive at a given point of a program p if
 - Exist a directed path from p to an use of v and
 - that path does not contain any definition of v



Liveness analysis algorithm

- 1. Identify which variables are define and which ones are read (used) by an instruction
 - GEN and KILL sets (local information)
- 2. Specify how instructions transmit live values around the program
 - How to compute IN and OUT sets from GEN and KILL sets (global information)
- 3. Iterate (2) until nothing (i.e., IN and OUT set) changes
 - Notice that (1) is performed only once!
 - GEN and KILL sets are constants and, therefore, path independent!

GEN and KILL sets

- GEN[i] = {all variables read (used) by instruction i}

```
%myVar3 <- %myVar1    // GEN[i] = {%myVar1}
```

- KILL[i] = {all variables defined by instruction i}

```
%myVar3 <- %myVar1    // KILL[i] = {%myVar3}
```

```
%myVar3 += %myVar1
```

```
KILL[i] = {%myVar3}   GEN[i] = {%myVar1, %myVar3}
```

GEN and KILL sets: more examples

- $GEN[i] = \{\text{all variables read (used) by instruction } i\}$
- $KILL[i] = \{\text{all variables defined by instruction } i\}$

`rdi++`

$KILL[i] = \{rdi\}$

$GEN[i] = \{rdi\}$

GEN and KILL sets: more examples

- $GEN[i] = \{\text{all variables read (used) by instruction } i\}$
- $KILL[i] = \{\text{all variables defined by instruction } i\}$

`cjump rdi <= %v2 :true`

$KILL[i] = \{ \}$

$GEN[i] = \{rdi, \%v2\}$

Liveness analysis algorithm

1. Define which variables are define and which ones are read (used) for each instruction
 - GEN and KILL sets

-
2. Specify how instructions transmit live values around the program
 - How to compute IN and OUT sets from GEN and KILL sets

3. Iterate (2) until nothing changes

IN and OUT sets

- $IN[i] = \{\text{all variables live right before instruction } i\}$

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$i: \%v2 \leftarrow \%v1$
If $OUT[i] = \{\}$ then
 $IN[i] = \{\%v1\}$

$i: \%v2 \leftarrow \%v1$
If $OUT[i] = \{\%v2\}$ then
 $IN[i] = \{\%v1\}$

- $OUT[i] = \{\text{all variables live right after instruction } i\}$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$

$i : \%v3 \leftarrow 5$
 $i+1: \%v2 \leftarrow \%v1$
If $IN[i+1] = \{\%v1\}$, then
 $OUT[i] = \{\%v1\}$

$i : \text{cjump } \%v = 1 :s2$
 $i+1: :s1$
 $i+j: :s2$
If $IN[i+1] = \{\%v1\}$
 $IN[i+j] = \{\%v2\}$,
Then $OUT[i] = \{\%v1, \%v2\}$

Algorithm

```
for (each instruction  $i$ ) {
```

```
    GEN[ $i$ ] = ...
```

```
    KILL[ $i$ ] = ...
```

```
}
```

```
for (each instruction  $i$ ) IN[ $i$ ] = OUT[ $i$ ] = { };
```

```
do{
```

```
    for (each instruction  $i$ ){
```

```
        IN[ $i$ ] = GEN[ $i$ ]  $\cup$  (OUT[ $i$ ] - KILL[ $i$ ])
```

```
        OUT[ $i$ ] =  $\cup_{s \text{ a successor of } i}$  IN[ $s$ ]
```

```
    }
```

```
} while (changes to any IN or OUT occur);
```

Outline

- Introduction to register allocation
- Liveness analysis
- Calling convention

Calling convention in GEN/KILL

	GEN	KILL
call u N	{ u, args used}	{ caller save registers}
call RUNTIME N	{ args used}	{ caller save registers}
return	{ rax, callee save registers}	{ }

The reason why call and return instructions must be treated with the above special rules will be explained at the next lecture

Let's run an example to show the computation of the liveness analysis

Code example

GEN

KILL

```
(@myF
```

```
0
```

```
%a <- 2 // 1
```

```
rax <- %a // 2
```

```
 return // 3
```

```
)
```

{?}

{?}

{?}

{?}

{?}

{?}

Calling convention in GEN/KILL

	GEN	KILL
call u N	{ u, args used}	{ caller save registers}
call RUNTIME N	{ args used}	{ caller save registers}
return	{ rax, callee save registers}	{ }

Registers

Arguments

rdi
rsi
rdx
rcx
r8
r9

Result

rax

Caller save

r10
r11
r8
r9
rax
rcx
rdi
rdx
rsi

Callee save

r12
r13
r14
r15
rbp
rbx

Registers

Arguments

rdi
rsi
rdx
rcx
r8
r9

Result

rax

Caller save

r10
r11
r8
r9
rax
rcx
rdi
rdx
rsi

Callee save

r12

*Let's assume
we only have 1 callee save register
(for keeping the example
as simple as possible)*

Algorithm

```
for (each instruction  $i$ ) {  
    GEN[ $i$ ] = ...  
    KILL[ $i$ ] = ...  
}  
for (each instruction  $i$ ) IN[ $i$ ] = OUT[ $i$ ] = { };  
do{  
    for (each instruction  $i$ ){  
        IN[ $i$ ] = GEN[ $i$ ]  $\cup$  (OUT[ $i$ ] - KILL[ $i$ ])  
        OUT[ $i$ ] =  $\cup_{s \text{ a successor of } i}$  IN[ $s$ ]  
    }  
} while (changes to any IN or OUT occur);
```

Code example

	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}		
rax <- %a // 2	{%a}	{rax}		
→ return // 3	{rax, r12}	{ }		
)				

GEN[i] = {all variables read (used) by instruction i}

KILL[i] = {all variables defined by instruction i}

Algorithm

```
for (each instruction  $i$ ) {
```

```
    GEN[ $i$ ] = ...
```

```
    KILL[ $i$ ] = ...
```

```
}
```

```
→ for (each instruction  $i$ ) IN[ $i$ ] = OUT[ $i$ ] = { };
```

```
do{
```

```
    for (each instruction  $i$ ){
```

```
        IN[ $i$ ] = GEN[ $i$ ]  $\cup$  (OUT[ $i$ ] - KILL[ $i$ ])
```

```
        OUT[ $i$ ] =  $\cup_{s \text{ a successor of } i}$  IN[ $s$ ]
```

```
    }
```

```
} while (changes to any IN or OUT occur);
```


Code example

	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}	{ }	{ }
rax <- %a // 2	{%a}	{rax}	{ }	{ }
return // 3	{rax, r12}	{ }	{ }	{ }
)				

Algorithm

```
for (each instruction  $i$ ) {
```

```
    GEN[ $i$ ] = ...
```

```
    KILL[ $i$ ] = ...
```

```
}
```

```
for (each instruction  $i$ ) IN[ $i$ ] = OUT[ $i$ ] = { };
```

```
→ do{
```

```
    for (each instruction  $i$ ){
```

```
        IN[ $i$ ] = GEN[ $i$ ]  $\cup$  (OUT[ $i$ ] - KILL[ $i$ ])
```

```
        OUT[ $i$ ] =  $\cup_{s \text{ a successor of } i}$  IN[ $s$ ]
```

```
    }
```

```
} while (changes to any IN or OUT occur);
```

Code example

	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}	{ }	{ }
rax <- %a // 2	{%a}	{rax}	{ }	{ }
→ return // 3	{rax, r12}	{ }	{ }	{ }
)				

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$

Code example

	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}	{ }	{ }
rax <- %a // 2	{%a}	{rax}	{ }	{ }
→ return // 3	{rax, r12}	{ }	{rax, r12}	{ }
)				

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$


Code example

	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}	{ }	{ }
→ rax <- %a // 2	{%a}	{rax}	{ }	{ }
return // 3	{rax, r12}	{ }	{rax, r12}	{ }
)				

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$

Code example

	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}	{ }	{ }
 rax <- %a // 2	{%a}	{rax}	{%a, r12}	{rax, r12}
return // 3	{rax, r12}	{ }	{rax, r12}	{ }
)				

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$

Code example

	GEN	KILL	IN	OUT
(@myF				
0				
→ %a <- 2 // 1	{ }	{%a}	{ }	{ }
rax <- %a // 2	{%a}	{rax}	{%a, r12}	{rax, r12}
return // 3	{rax, r12}	{ }	{rax, r12}	{ }
)				

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$

Code example

	GEN	KILL	IN	OUT
(@myF				
0				
→ %a <- 2 // 1	{ }	{%a}	{r12}	{%a, r12}
rax <- %a // 2	{%a}	{rax}	{%a, r12}	{rax, r12}
return // 3	{rax, r12}	{ }	{rax, r12}	{ }
)				

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$

Algorithm

```
for (each instruction  $i$ ) {
```

```
    GEN[ $i$ ] = ...
```

```
    KILL[ $i$ ] = ...
```

```
}
```

```
for (each instruction  $i$ ) IN[ $i$ ] = OUT[ $i$ ] = { };
```

```
do{
```

```
    for (each instruction  $i$ ){
```

```
        IN[ $i$ ] = GEN[ $i$ ]  $\cup$  (OUT[ $i$ ] - KILL[ $i$ ])
```

```
        OUT[ $i$ ] =  $\cup_{s \text{ a successor of } i}$  IN[ $s$ ]
```

```
    }
```

```
→ } while (changes to any IN or OUT occur);
```

Code example

	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}	{r12}	{%a, r12}
rax <- %a // 2	{%a}	{rax}	{%a, r12}	{rax, r12}
→ return // 3	{rax, r12}	{ }	{rax, r12}	{ }
)				

$$IN[i] = GEN[i] \cup (OUT[i] - KILL[i])$$

$$OUT[i] = \bigcup_{s \text{ a successor of } i} IN[s]$$

Algorithm

```
for (each instruction  $i$ ) {
```

```
    GEN[ $i$ ] = ...
```

```
    KILL[ $i$ ] = ...
```

```
}
```

```
for (each instruction  $i$ ) IN[ $i$ ] = OUT[ $i$ ] = { };
```

```
do{
```

```
    for (each instruction  $i$ ){
```

```
        IN[ $i$ ] = GEN[ $i$ ]  $\cup$  (OUT[ $i$ ] - KILL[ $i$ ])
```

```
        OUT[ $i$ ] =  $\cup_{s \text{ a successor of } i}$  IN[ $s$ ]
```

```
    }
```

```
→ } while (changes to any IN or OUT occur);
```

Code example

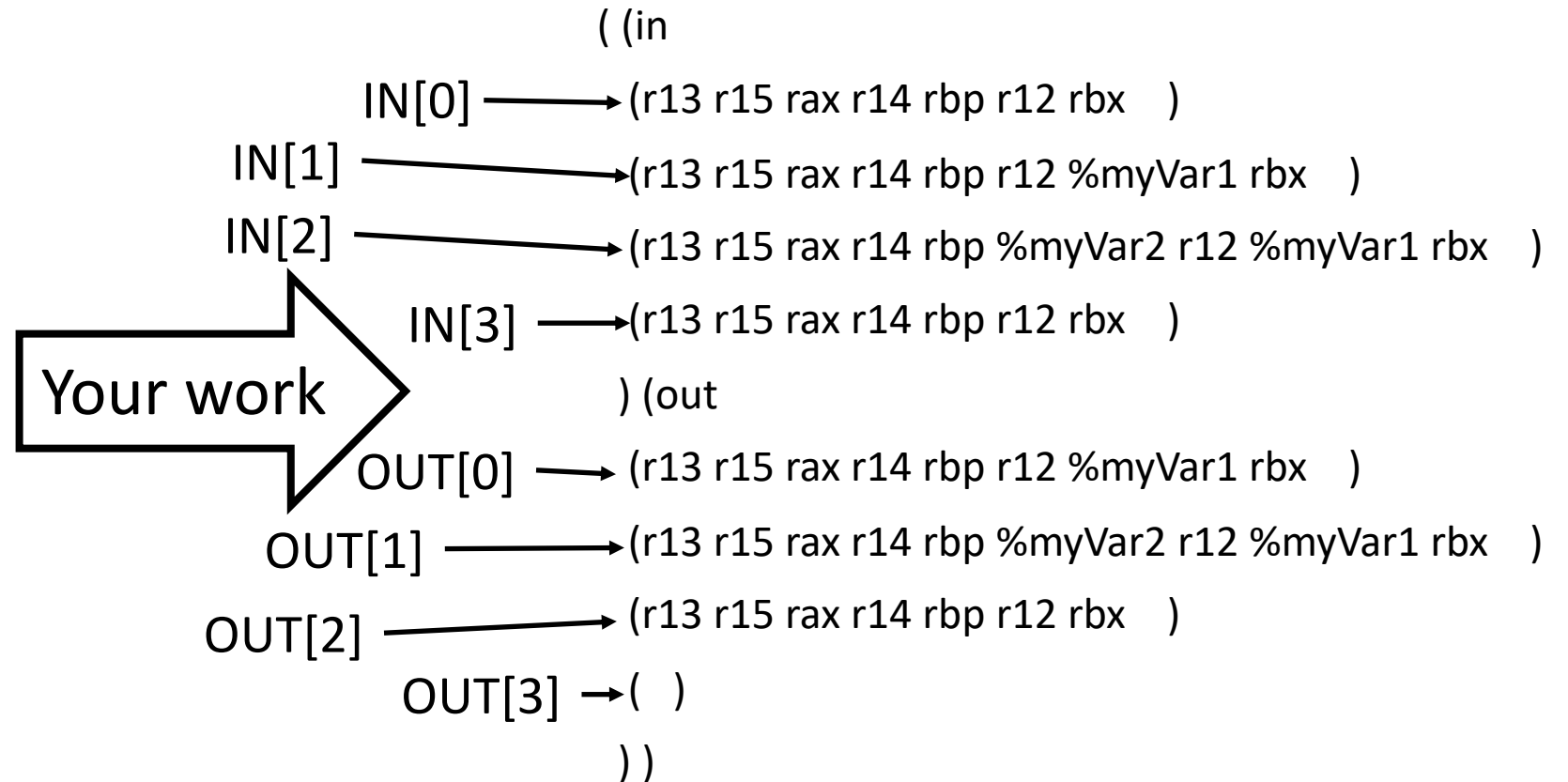
	GEN	KILL	IN	OUT
(@myF				
0				
%a <- 2 // 1	{ }	{%a}	{r12}	{%a, r12}
rax <- %a // 2	{%a}	{rax}	{%a, r12}	{rax, r12}
return // 3	{rax, r12}	{ }	{rax, r12}	{ }
)				

- Variables within the same set are alive at the same time at that point in the code
- Hence, they cannot be placed in the same register

Homework #1

- Compute the IN and OUT sets of all instructions of an L2 function given as input

```
(@myF
0
%myVar1 <- 5
%myVar2 <- 0
%myVar2 += %myVar1
return
)
```



Testing your homework #1

- Under L2/tests/liveness there are the tests you have to pass
- A new compiler argument: -l
 - Check L2compiler.cpp on Canvas
- To test:
 - To check all tests: make test_liveness
 - To check one test: ./liveness test/liveness/test1.L2f
- Check out each input/output for each test if you have doubts
 - For example, the correct output for the test
test/liveness/test1.L2f
is
test/liveness/test1.L2f.out

Debugging suggestion

- Don't forget you have our L2 compiler binary
- So, to help you debug your work:
 - you can write your own test (a new MyTest.L2f)
 - Generate the output of our L2 compiler by invoking `./liveness MyTest.L2f > MyTest.L2f.out`
 - Compare our output with the output generated by your L2 compiler

Always have faith in your ability

Success will come your way eventually

Best of luck!