

# **Higher-Order Functions (Part II)**

# FAE with Deferred Substitution

(interp {{with {y 10} {fun {x} {+ y x}}}})  
    {{with {y 7} y}})

Argument expression:

(interp {with {y 7} y})

⇒

(interp y) ⇒ 7

Function expression:

(interp {with {y 10} {fun {x} {+ y x}}})

⇒

(interp {fun {x} {+ y x}}) ⇒ ?

# FAE Values

A function value needs to keep its deferred substitution

```
(define-type FAE-Value
  [numV (n number?)]
  [closureV (param-name symbol?)
             (body FAE?)
             (ds DefSub?)]))
```

```
(define-type DefSub
  [mtSub]
  [aSub (name symbol?)
        (value FAE-Value?)
        (rest DefSub?)]))
```

```
(test (interp {with {y 10} {fun {x} {+ y x}}}))  
      (closureV 'x {+ y x}  
                (aSub 'y (num 10) (mtSub))))
```

# Continuing Evaluation

Function: `{ fun {x} {+ y x} }`

Argument: `7`

`y = 10`

To apply, interpret the function body with the given argument:

`(interp {+ y x})`

`x = 7`      `y = 10`

# FAE Interpreter with Deferred Substitution

```
; interp : FAE? DefSub? -> FAE-Value?
(define (interp a-fae ds)
  (type-case FAE a-fae
    [num (n) (numV n)]
    [add (l r) (num+ (interp l ds) (interp r ds))]
    [sub (l r) (num- (interp l ds) (interp r ds))]
    [id (name) (lookup name ds)]
    [fun (param-name body)
        (closureV param-name body ds)]
    [app (fun-expr arg-expr)
        (define fun-val
          (interp fun-expr ds))
        (define arg-val
          (interp arg-expr ds))
        (interp (closureV-body fun-val)
               (aSub (closureV-param-name fun-val)
                     arg-val
                     (closureV-ds fun-val))))]))
```