

Types

"Good" vs. "Bad" Expressions

`; interp-expr : FAE? ... -> FAE-Value?`

- Does `interp-expr` produce a value for all expressions?
- Of course not!
- `(interp-expr (parse '{5 5}))` etc ...
- But do we know enough about expressions to tell before actually calling `interp-expr`?

Quiz

- **Question #1:** What is the value of the following expression?

{ + 1 2 }

- **Answer: 3**

Quiz

- **Question #2:** What is the value of the following expression?

`{+ fun 17 8}`

- **Wrong answer: error**
- **Answer:** Trick question! `{+ fun 17 8}` is not an expression

Language Grammar for Quiz

```
<MFAE> ::= <num>
| true
| false
| {+ <MFAE> <MFAE>}
| {- <MFAE> <MFAE>}
| {= <MFAE> <MFAE>}
| <id>
| {fun {<id>*} <MFAE>}
| {<MFAE> <MFAE>*}
| {if <MFAE> <MFAE> <MFAE>}
```

Quiz

- **Question #3:** Is the following an expression?

`{{fun {x y} 1} 7}`

- **Wrong answer: No**
- **Answer: Yes** (according to our grammar)

Quiz

- **Question #4:** What is the value of the following expression?

`{{fun {x y} 1} 7}`

- **Answer:** `{fun {y} 1}` (according to some interpreters)
- But no *real* language would accept `{{fun {x y} 1} 7}`
- Let's agree to call `{{fun {x y} 1} 7}` an ***ill-formed expression*** because `{fun {x y} 1}` should be used only with two arguments
- Let's agree to never evaluate ill-formed expressions

Quiz

- **Question #5:** What is the value of the following expression?

```
{{fun {x y} 1} 7}
```

- **Answer: None** - the expression is ill-formed

Quiz

- **Question #6:** Is the following a well-formed expression?

`{+ {fun {} 1} 8}`

- **Answer: Yes** (according to our definition of well-formed)

Quiz

- **Question #7:** What is the value of the following expression?

```
{+ {fun {} 1} 8}
```

- **Answer: None** - it produces an error:

numeric operation expected number

- Let's agree that a **fun** expression cannot be inside a **+** form

Quiz

- **Question #8:** Is the following a well-formed expression?

`{+ {fun {} 1} 8}`

- **Answer: No** (according to our new definition)

Quiz

- **Question #9:** Is the following a well-formed expression?

{+ {{fun {x} x} 7} 5}

- **Answer:** Depends on what we meant by *inside* in our most recent agreement
 - *Anywhere inside* - **No**
 - *Immediately inside* - **Yes**
- Since our interpreter produces **12**, and since that result makes sense, let's agree on *immediately inside*

Quiz

- **Question #10:** Is the following a well-formed expression?

```
{+ {{fun {x} x} {fun {y} y}} 5}
```

- **Answer:** **Yes**, but we don't want it to be!

Quiz

- **Question #11:** Is it possible to define **well-formed** (as a decidable property) so that we reject all expressions that produce errors?
- **Answer: Yes:** reject *all* expressions!

Quiz

- **Question #12:** Is it possible to define **well-formed** (as a decidable property) so that we reject *only* expressions that produce errors?
- **Answer: No**

```
{+ 1 {if ... 1 {fun {x} x}}}
```

- If we always knew whether ... produces true or false, we could solve the halting problem
- See also: Rice's theorem: all *non-trivial, semantic* properties of programs are undecidable

Types

- Solution to our dilemma
 - In the process of rejecting expressions that are certainly bad, also reject some expressions that are good

```
{+ 1 {if {prime? 131101}
        1
        {fun {x} x}}}
```

- It's a tradeoff: do we care more about rejecting bad programs, or about not rejecting good ones?
 - Different languages pick different tradeoffs
 - **Typed:** Java, Scala, Haskell, etc.
 - **Untyped:** Racket, Python, Javascript, etc.
 - AKA dynamically typed

Types

- Overall strategy:
 - Assign a **type** to each expression *without evaluating*
 - Compute the type of a complex expression based on the types of its subexpressions

Types

`1` : *number*

`true` : *boolean*

